

EMPIRICALLY IDENTIFYING THE BEST GENETIC ALGORITHM FOR COVERING ARRAY GENERATION

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Combinatorial Testing

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Modern software systems are highly configurable and involve many interacting parameters

Combinatorial testing is a widely used and practical technique for detecting failures caused by the parameter interactions

One of the key challenges in combinatorial testing is covering array generation, which is an noteworthy area of research

From Kuhn et al., 70% of failures can be detected by 2-way interactions of the software system's parameters

Covering arrays can save testing time while still detecting many important software faults

Combinatorial Testing

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2-way Covering Arrays

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Suppose there are 4 parameters (pa_1 , pa_2 , pa_3 , and pa_4) in a system under test (SUT), each with 3 values (0, 1, 2)

If we want to cover all 54 pair-wise interactions between every 2 parameters in the SUT, then only 9 test cases are needed

What is the most efficient and effective method for **generating** covering arrays?

Table 1. Covering array of the SUT.

pa_1	pa_2	pa_3	pa_4
0	0	0	0
1	0	2	1
2	1	2	0
2	0	1	2
1	1	0	2
0	1	1	1
2	2	0	1
1	2	1	0
0	2	2	2

2-way Covering Arrays

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0	1	1	1
2	2	0	1
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0	2	2	2

Covering Array Generation

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Mathematical and Greedy Methods

- OFOT: One Factor One Time Method
- AETG: Automatic Efficient Tests Generator

Evolutionary Search Techniques

- Particle swarm optimization
- Simulated annealing
- Ant colony optimization

Covering Array Generation

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Covering Array Generation

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Mathematical and Greedy Methods

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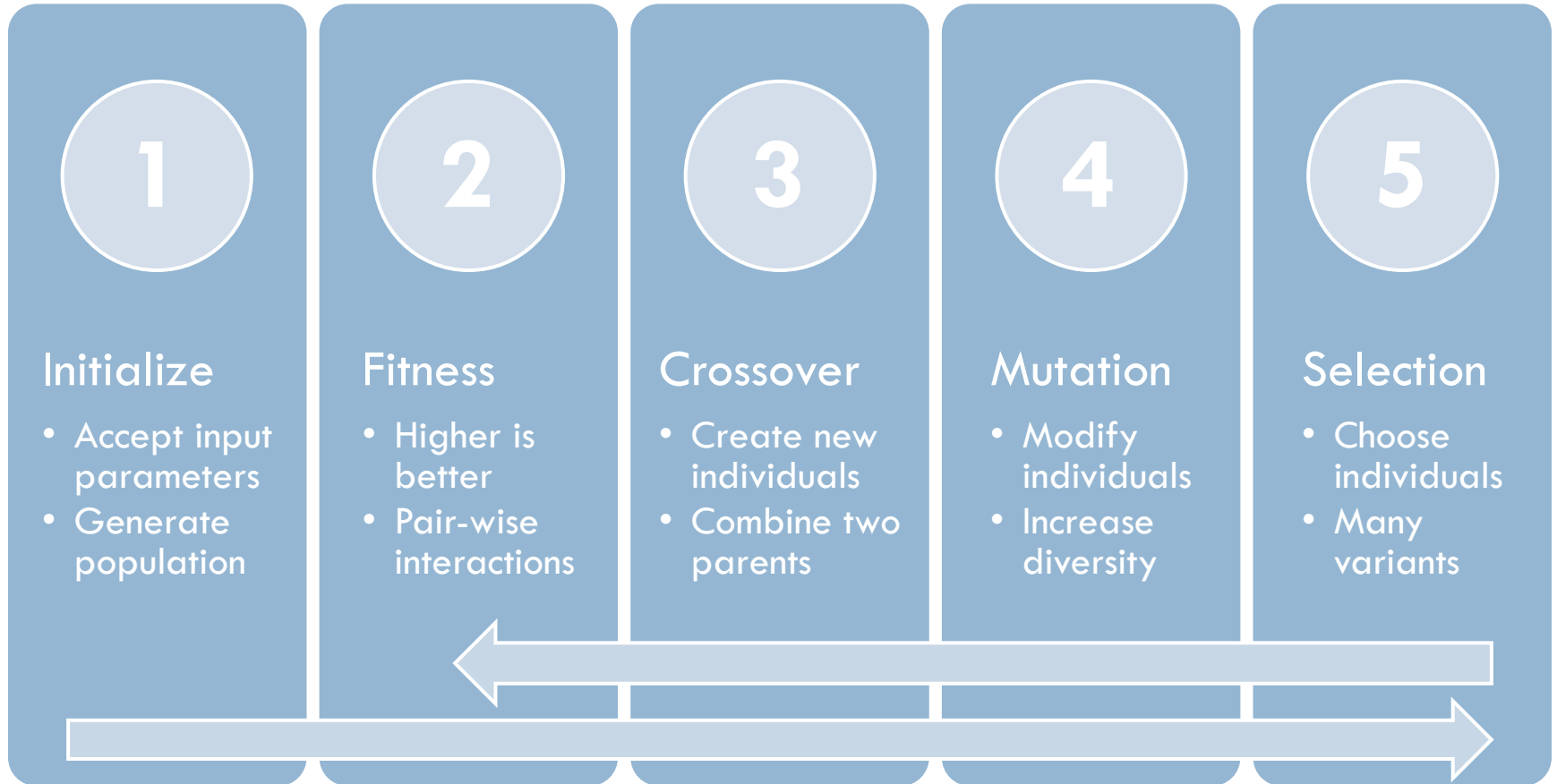
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This paper studies and improves genetic algorithms for covering array generation

Genetic Algorithm Phases

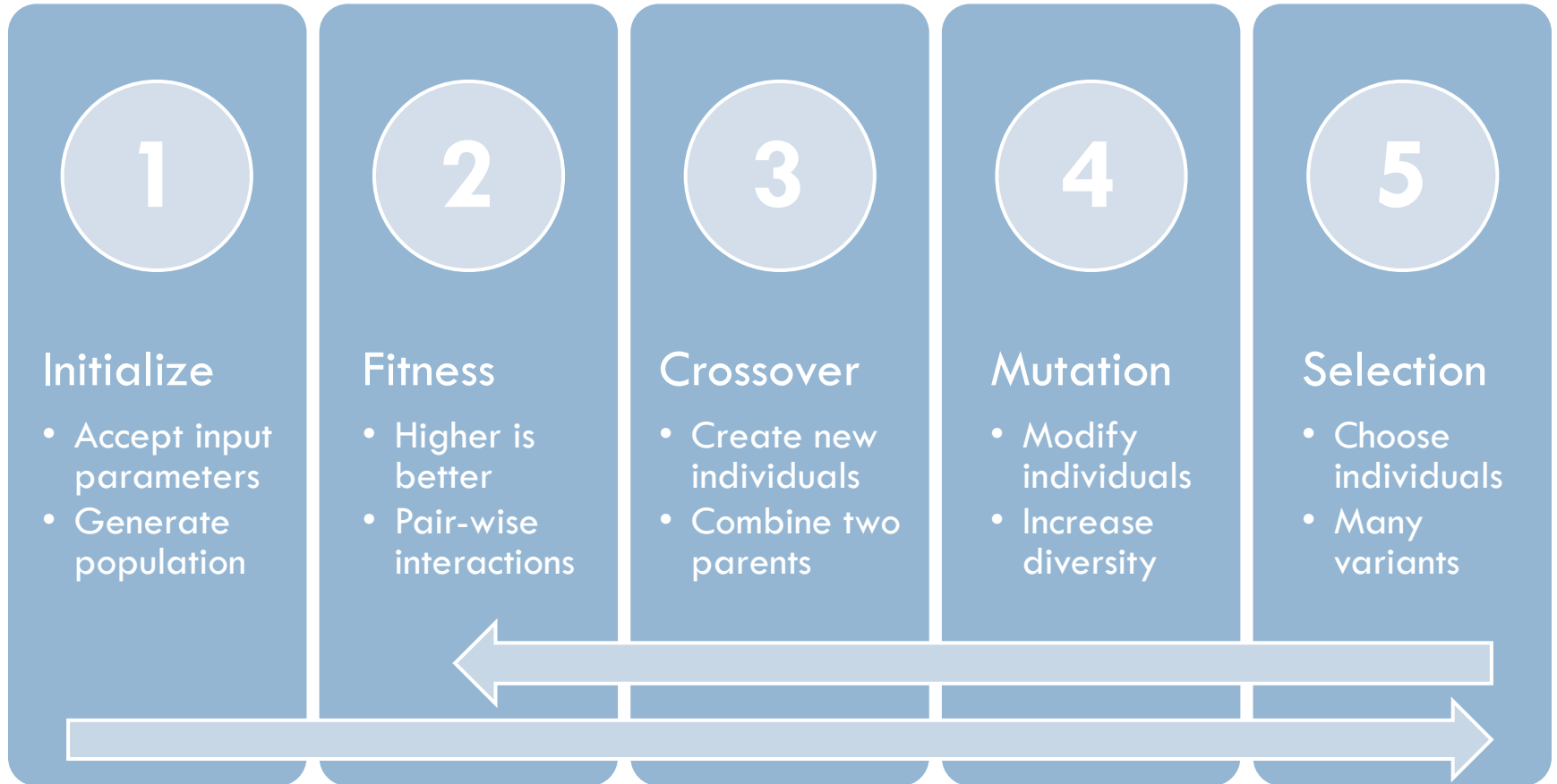
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Genetic algorithms solve complex problems

Genetic Algorithm Phases

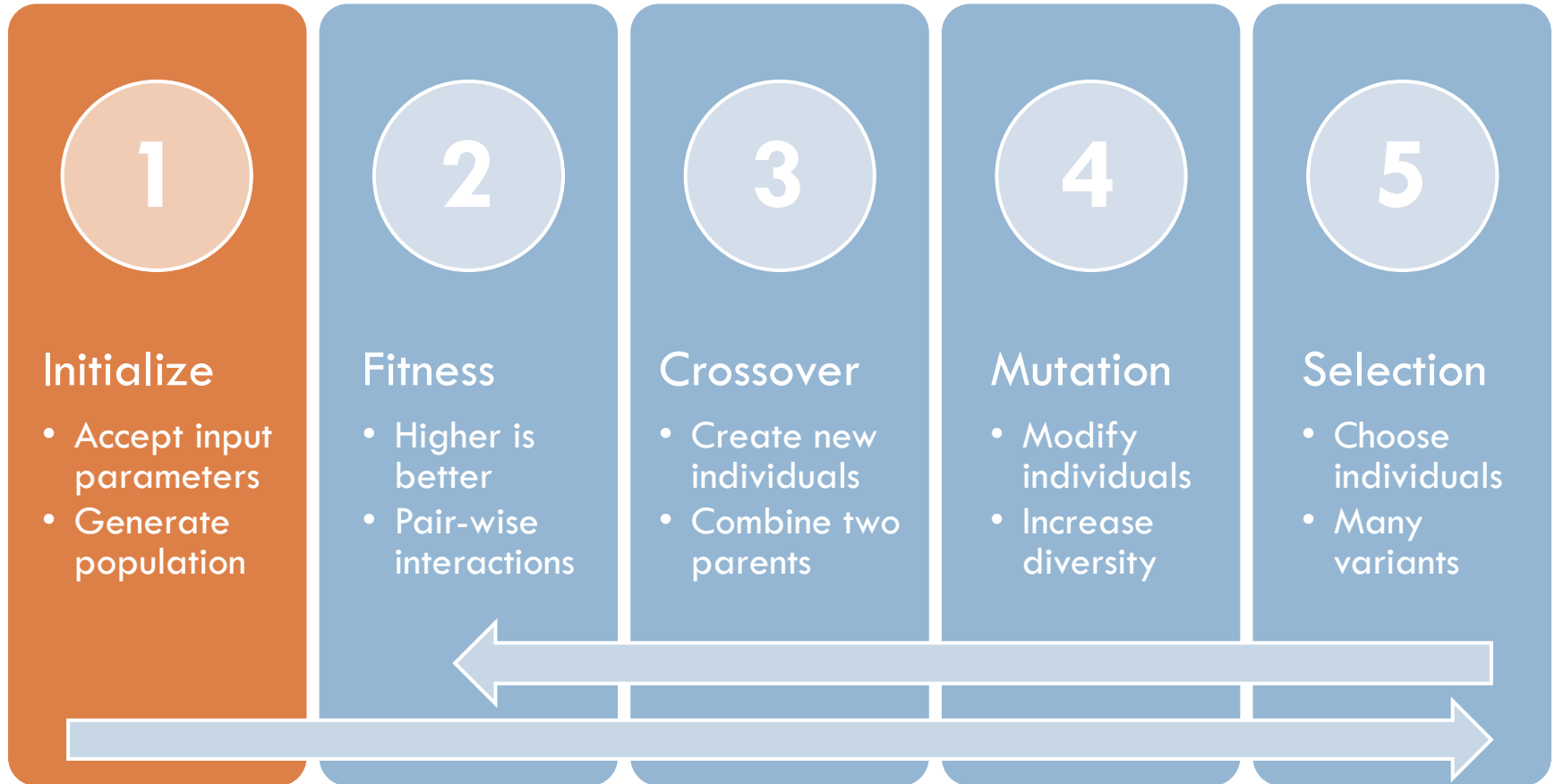
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Genetic algorithms are hard to configure

Genetic Algorithm Parameters

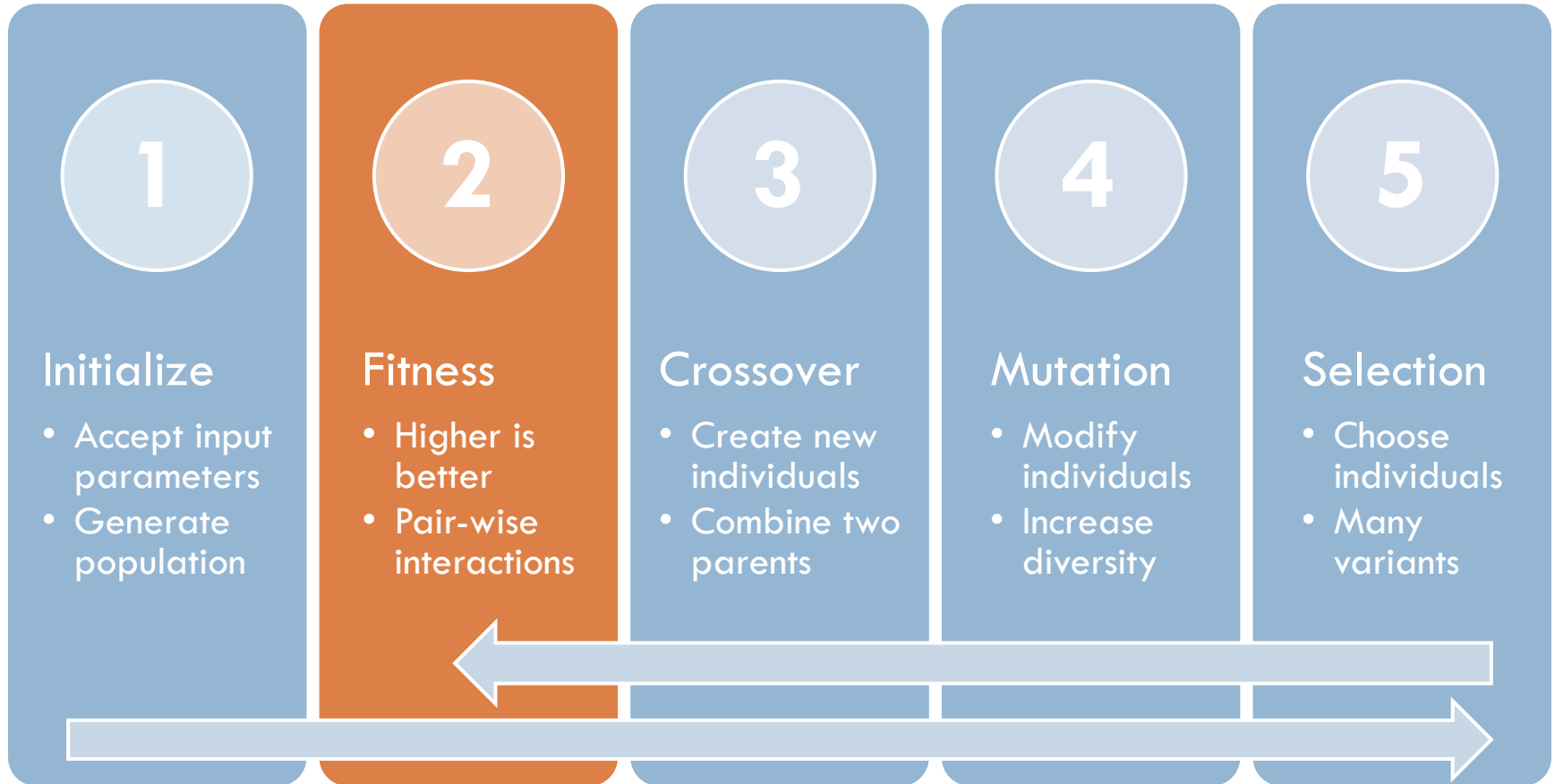
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System under test (SUT) description (e.g., 3^{13})

Genetic Algorithm Parameters

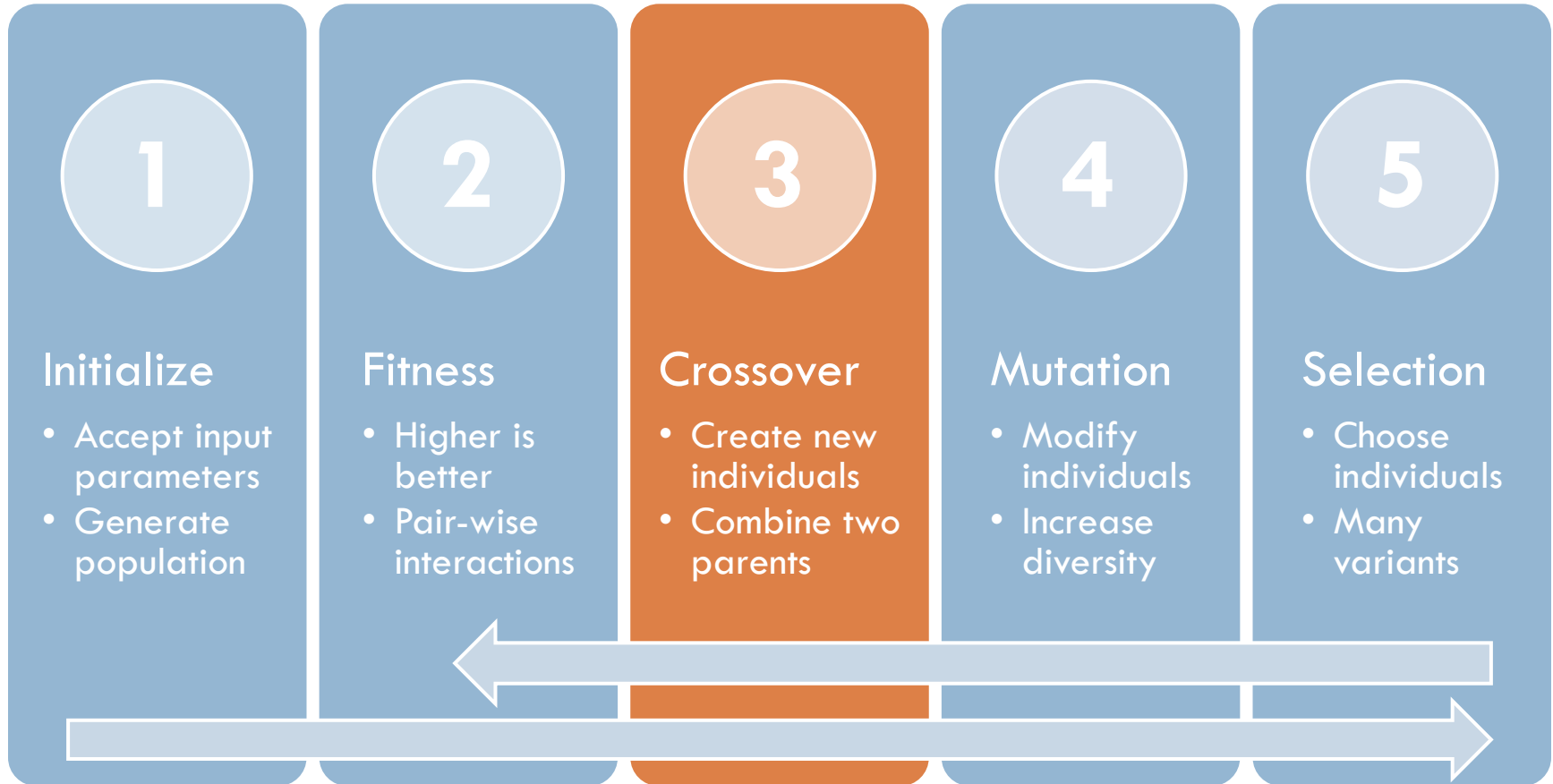
15



Number of uncovered pair-wise interactions

Genetic Algorithm Parameters

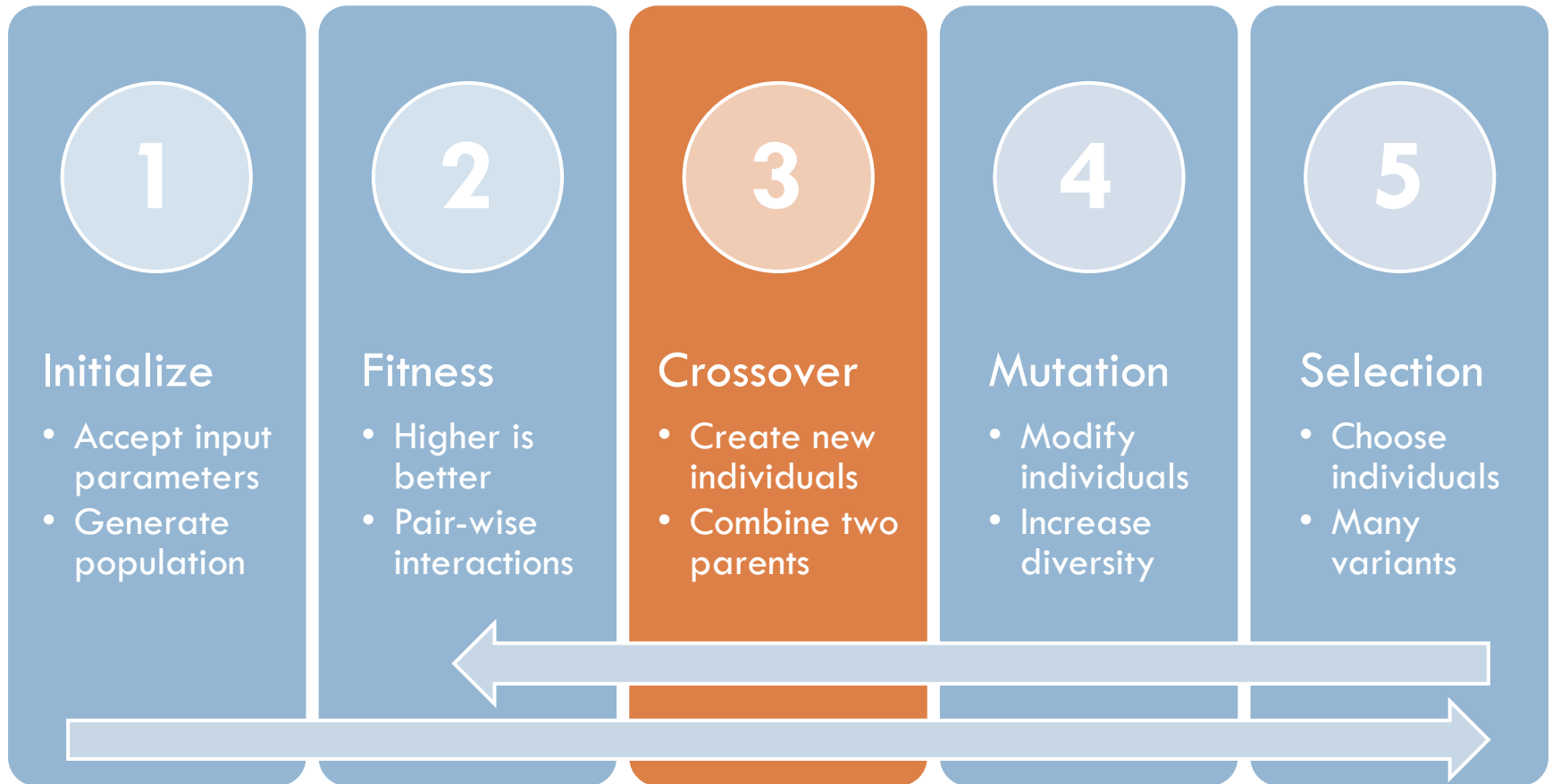
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P_c controls the probability of crossover

Genetic Algorithm Parameters

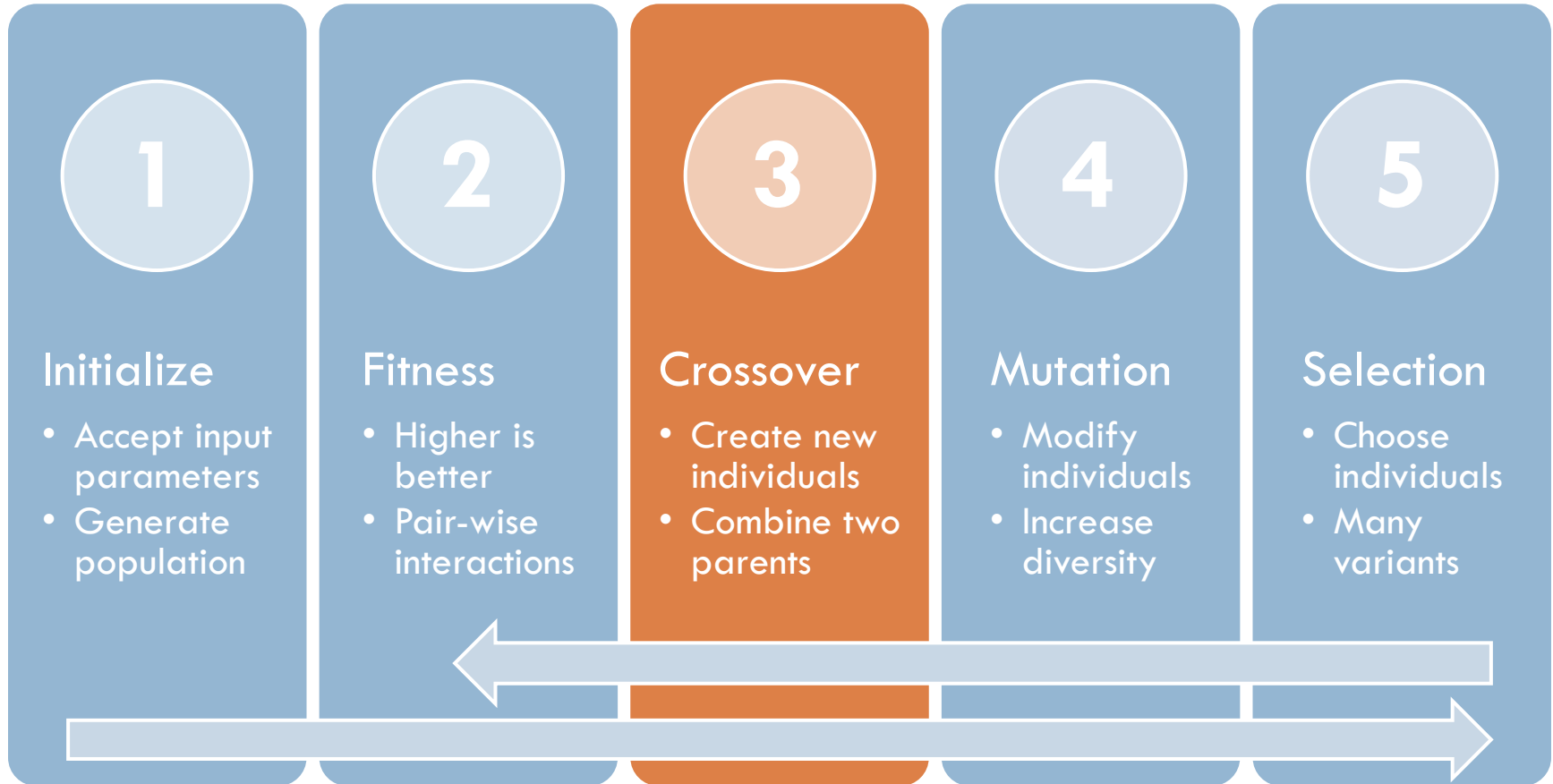
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If P_c is too high, then break good individuals

Genetic Algorithm Parameters

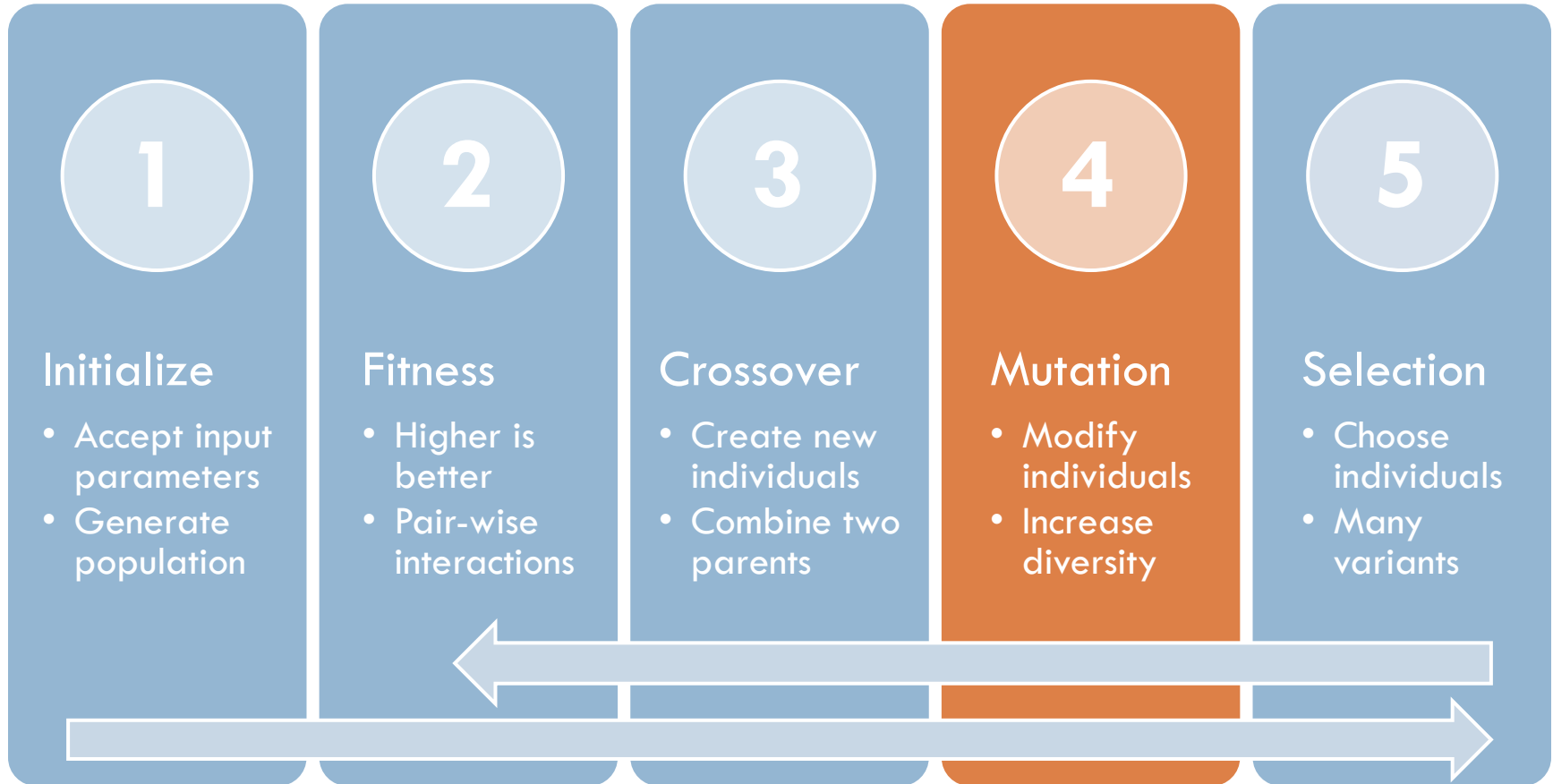
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If P_c is too low, then miss good solutions

Genetic Algorithm Parameters

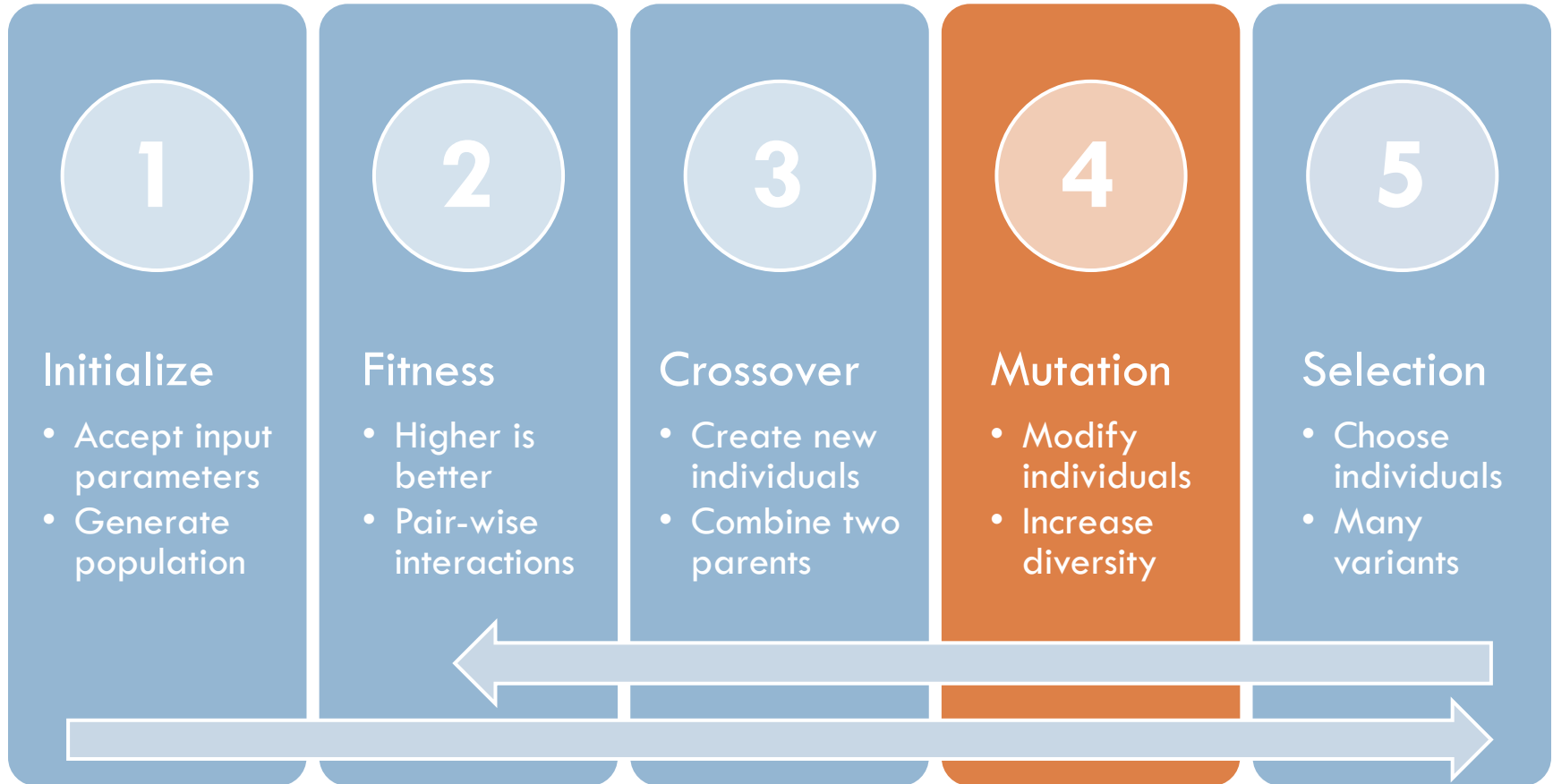
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P_m controls the probability of mutation

Genetic Algorithm Parameters

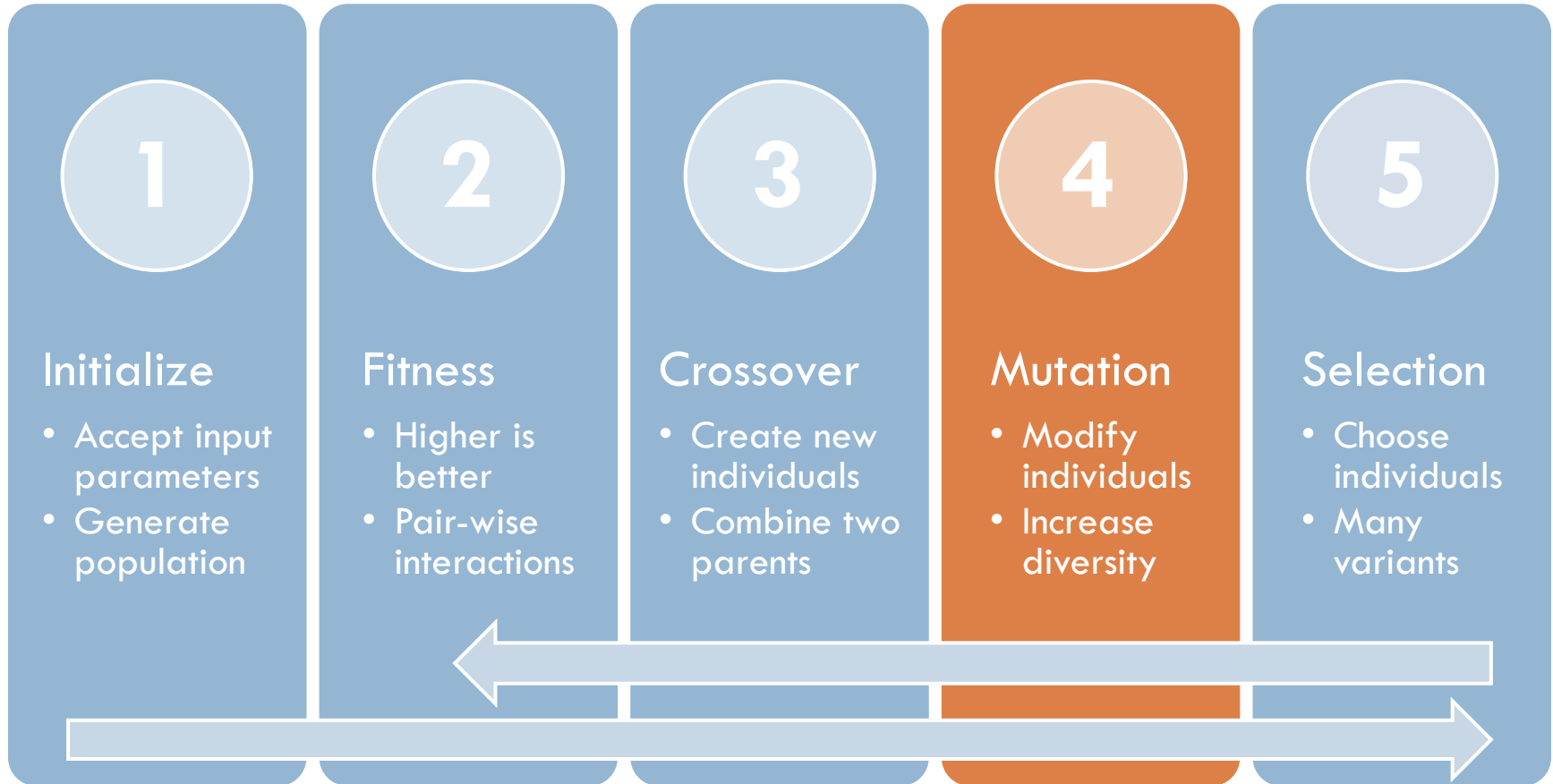
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If P_m is too small, then cannot escape minima

Genetic Algorithm Parameters

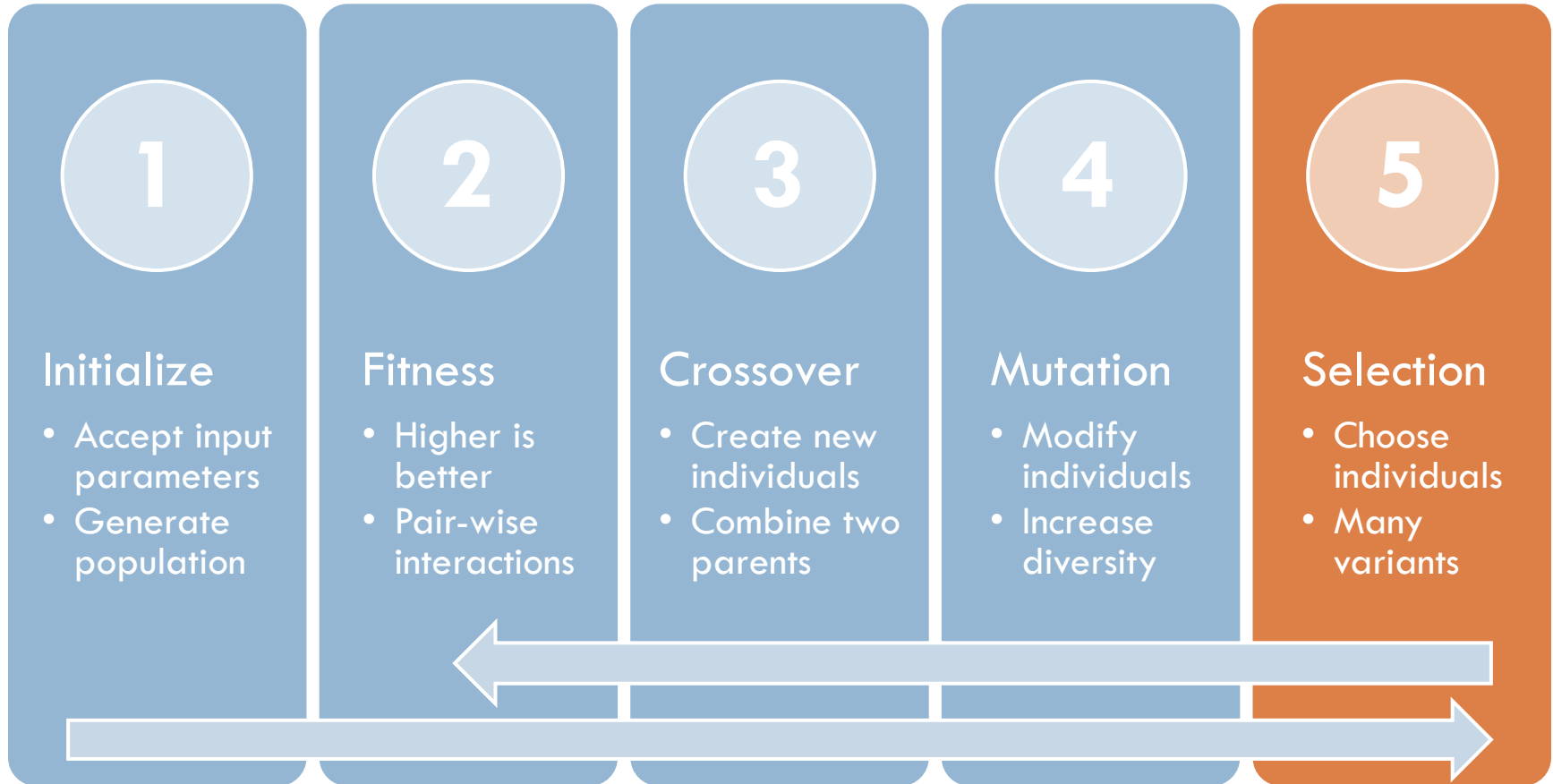
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If P_m is too large, then degrade into random

Genetic Algorithm Parameters

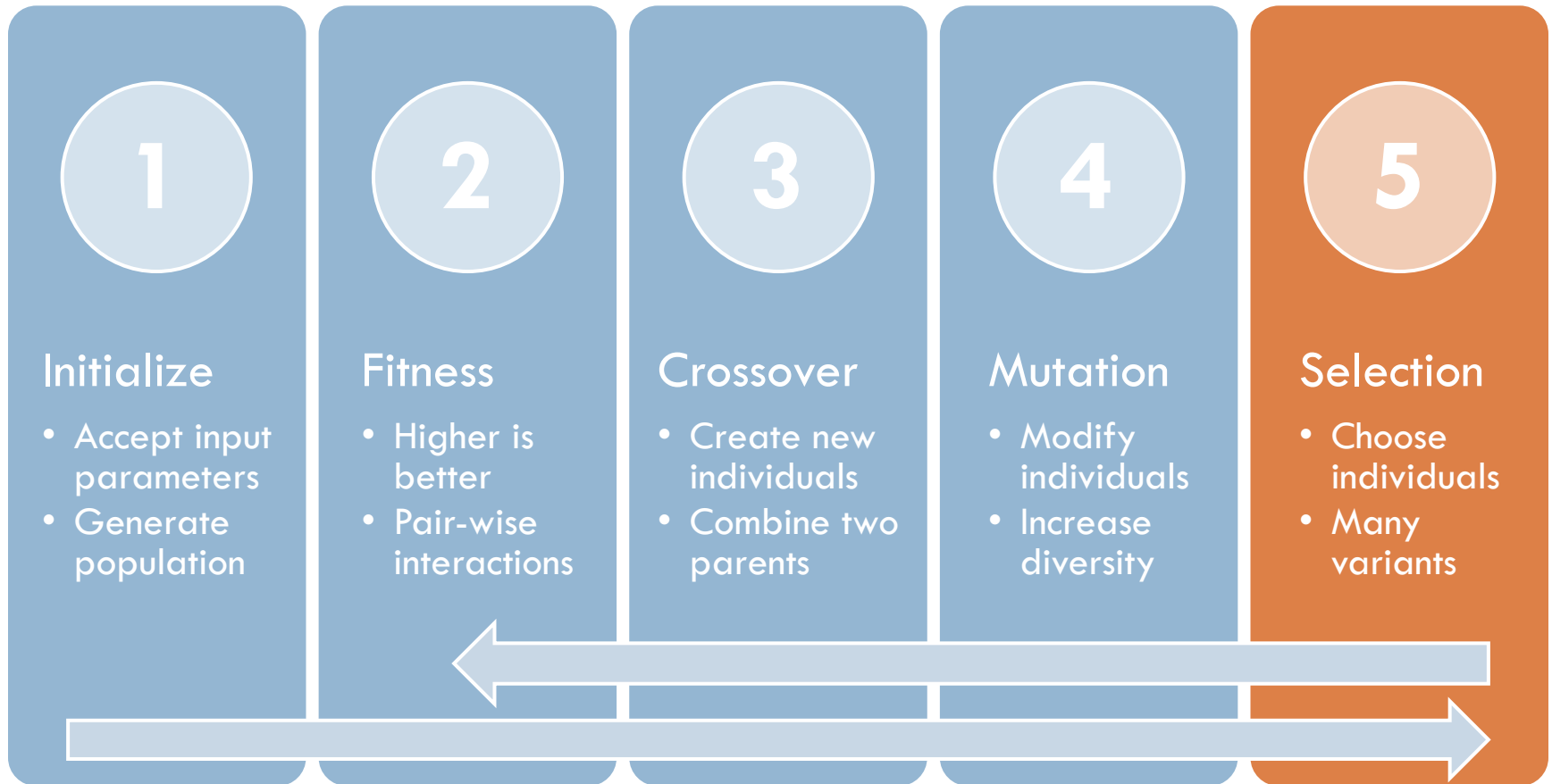
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Standard GA: Select the superior individuals

Genetic Algorithm Parameters

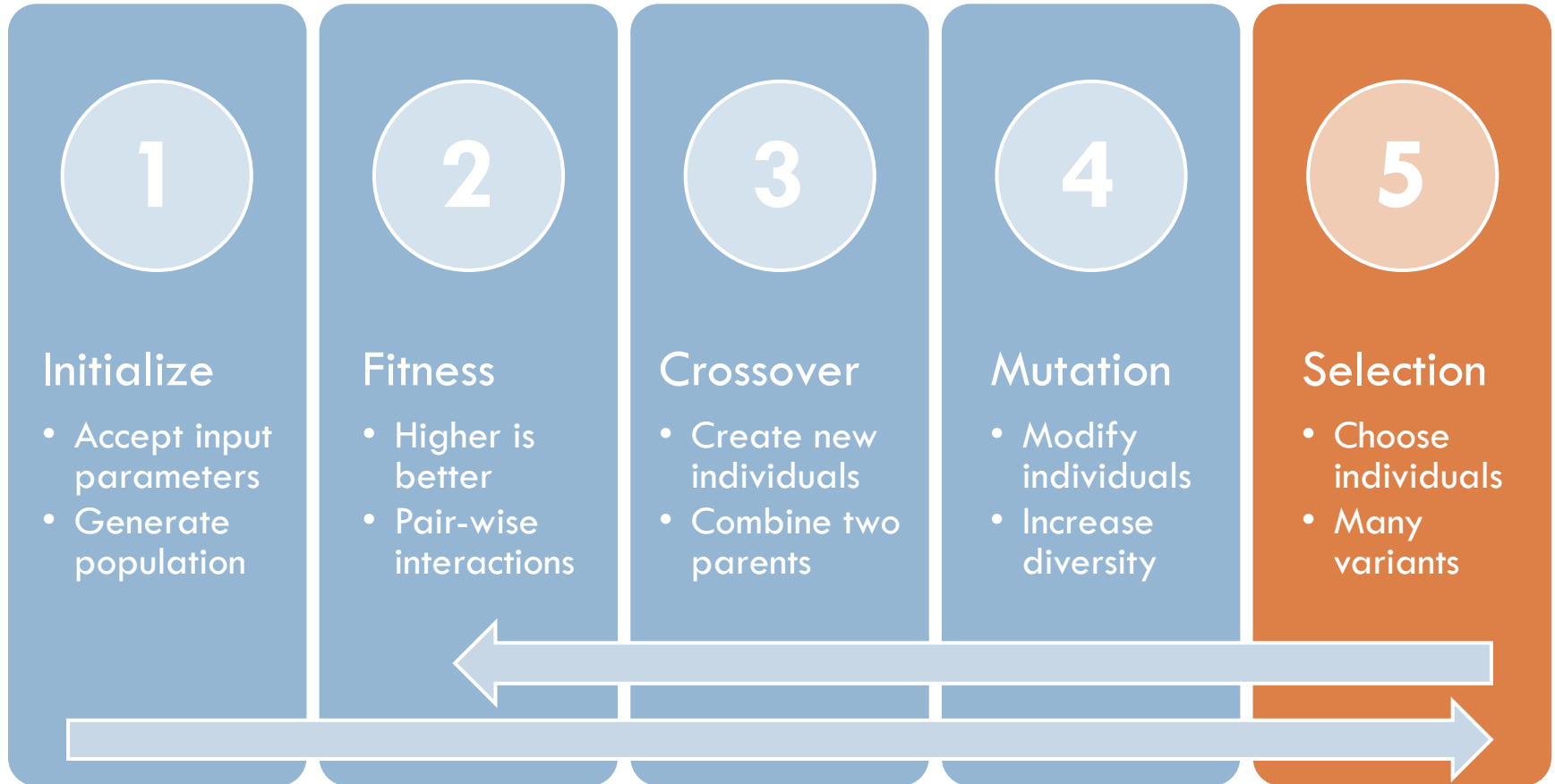
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GA-: Select the inferior individuals

Genetic Algorithm Parameters

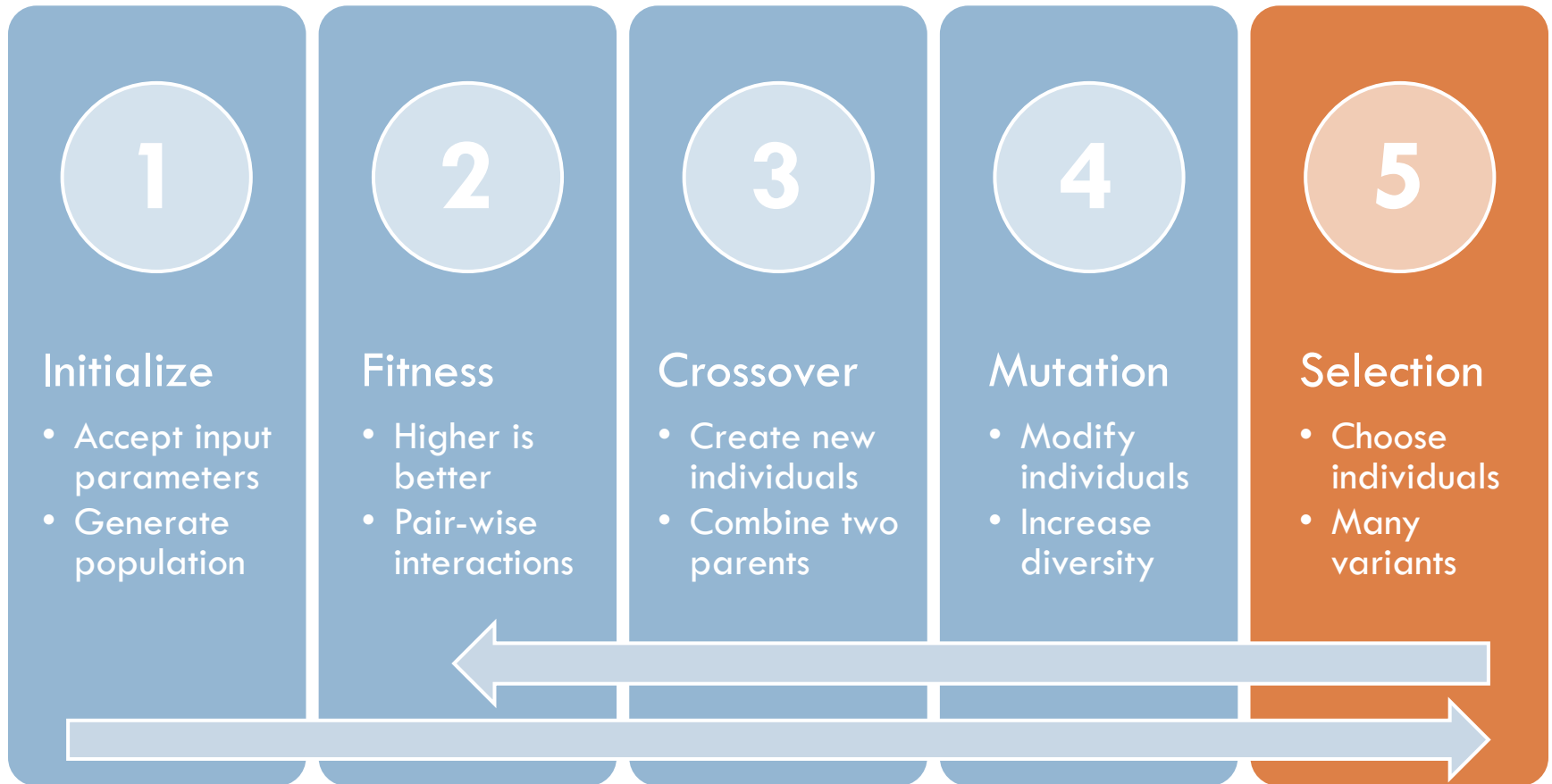
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GA: Randomly select the individuals

Genetic Algorithm Parameters

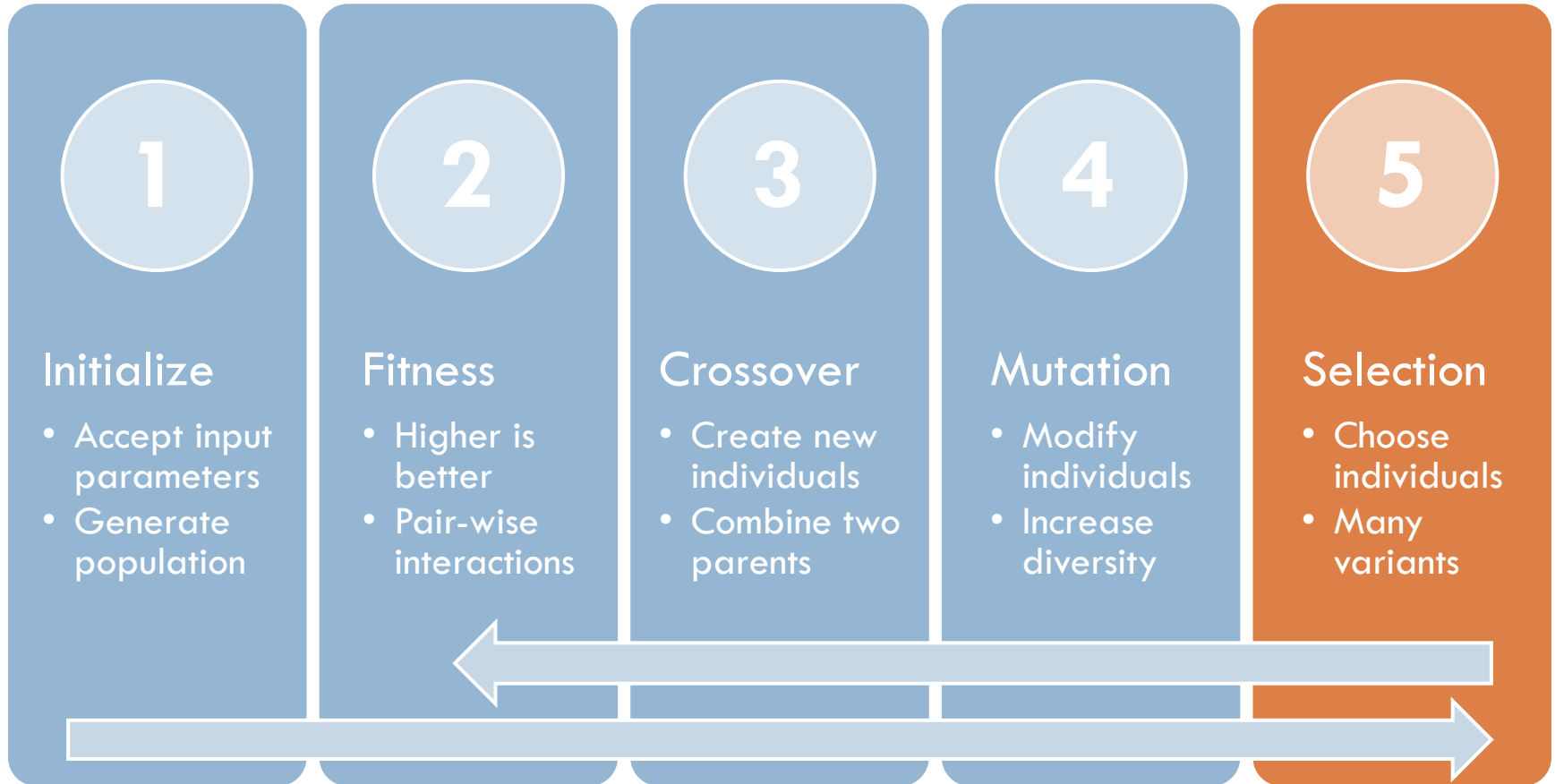
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GA climb: Use elitism to keep best individual

Genetic Algorithm Parameters

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GA, GA-, GAr, GA climb, GA- climb, GAr climb

Experimental Design

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Population Size

Number of
Generations

Crossover
Probability

Mutation
Probability

Experimental Design

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Population Size

- 100, 2100,
- 4100, 6100

Number of
Generations

Crossover
Probability

Mutation
Probability

Experimental Design

29

Population Size

Number of
Generations

- 100, 600, 1100

Crossover
Probability

Mutation
Probability

Experimental Design

30

Population Size

Number of
Generations

Crossover
Probability

Mutation
Probability

- 0.2, 0.4, 0.6, 0.8, 1.0

Experimental Design

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Population Size

Number of
Generations

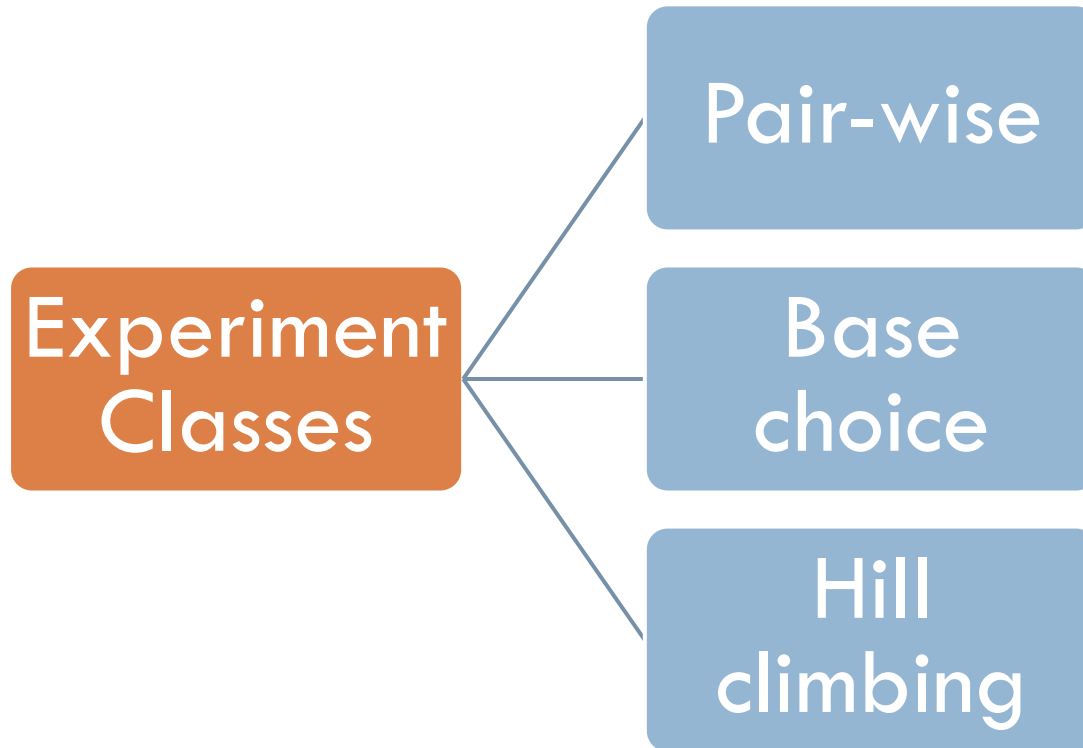
Crossover
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Experimental Design

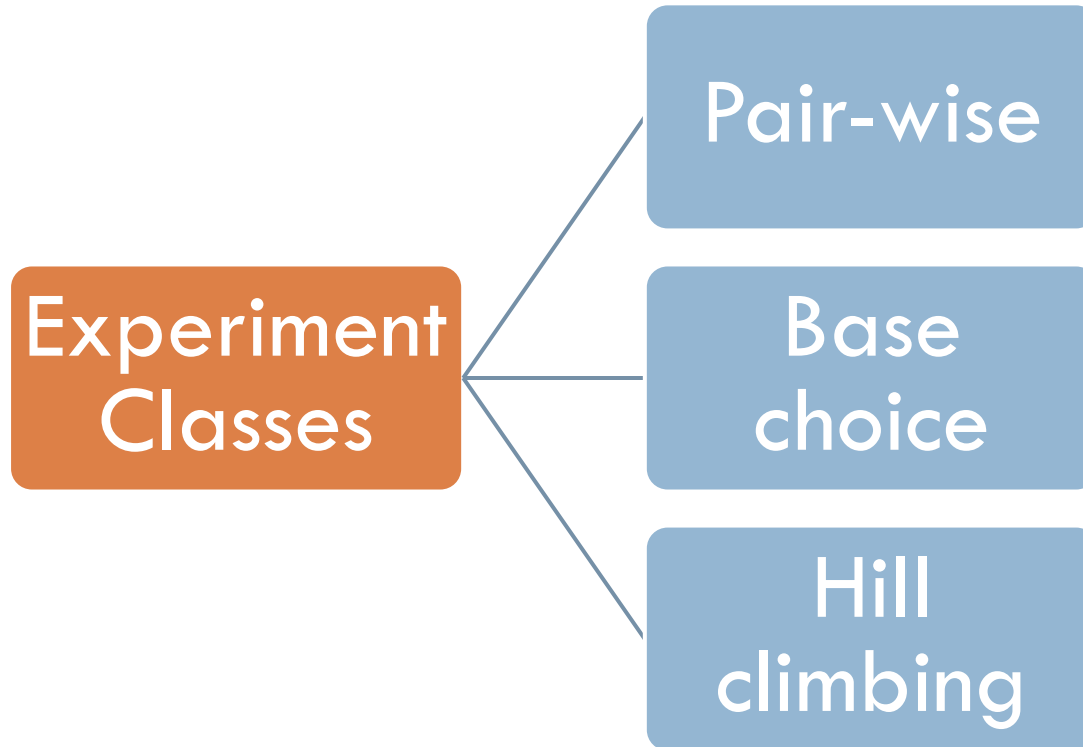
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Is there an improved configuration of genetic algorithm for a particular pair-wise SUT?

Experimental Design

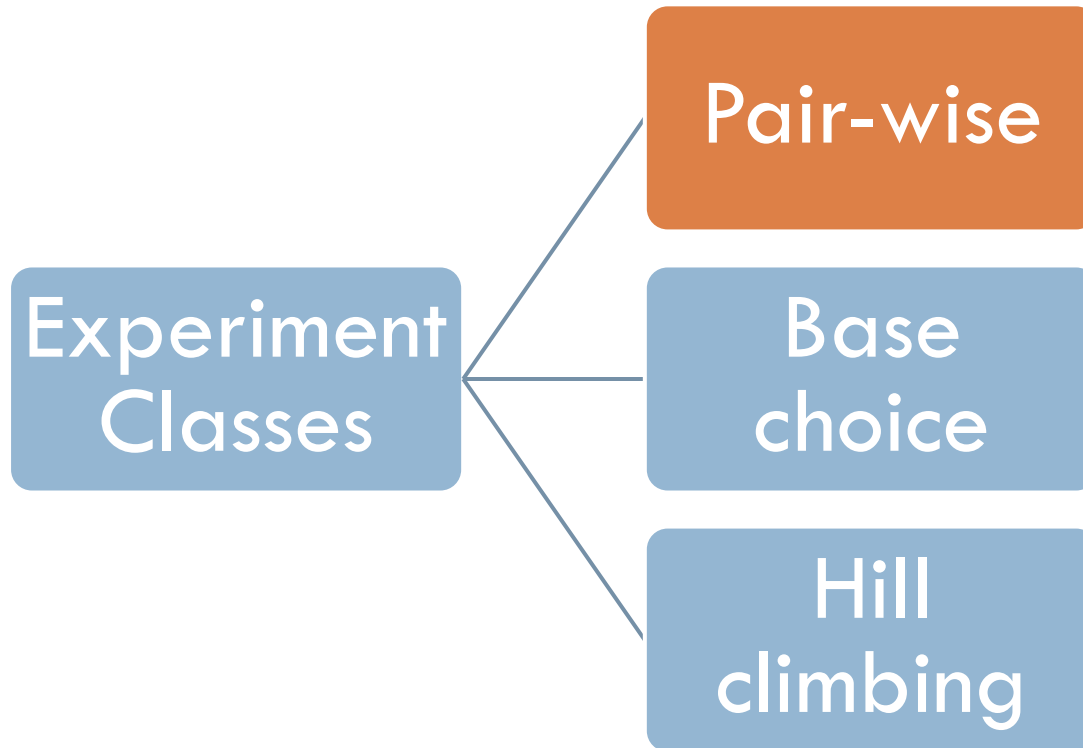
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Is there a common improved configuration for all pair-wise SUTs?

Experimental Design

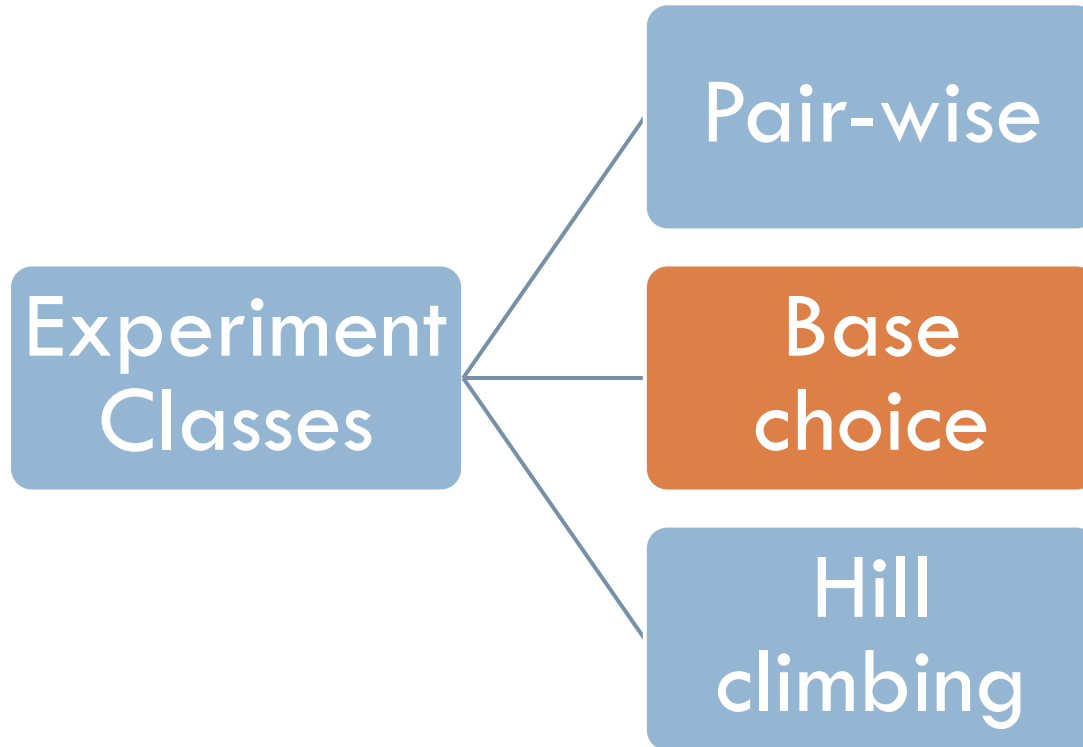
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Produce a 2-way covering array with 34 configurations and input into the next phases

Experimental Design

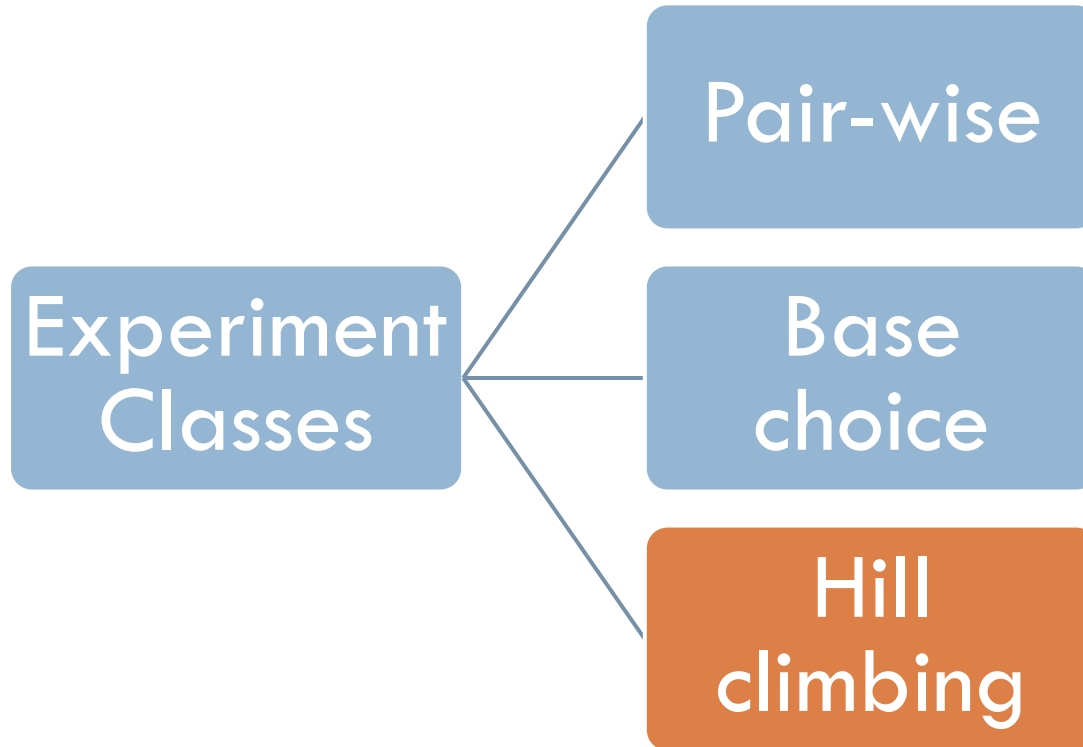
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Create configurations by changing the value of one parameter and not modifying others

Experimental Design

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Iteratively refine the configurations in order to find the best one for each SUT

Experimental Results

Table 3. The configurations of 15 SUTs improved by the three experiments.

SUT	VGA	m	G	P_c	P_m	CA Size	Run Time	SUT	VGA	m	G	P_c	P_m	CA Size	Run Time
4^{10}	GAr climb	100	100	0.2	0.2	28	0.234s	6^{30}	GA climb	100	1100	0.2	0.2	87	52.6s
3^{13}	GAr climb	100	1100	0.8	0.2	17	2.28s	10^{11}	GA climb	100	1100	0.8	0.2	154	19.8s
6^{10}	GA climb	6100	1100	0.2	0.2	58	402s	$7^6 6^7 5^6$	GAr climb	100	1100	0.8	0.2	82	23.5s
4^{20}	GAr climb	100	1100	0.8	0.2	35	10.1s	$8^2 7^2 6^2 5^2$	GA- climb	2100	600	0.8	0.6	70	277s
8^{10}	GA climb	2100	600	0.6	0.2	98	604s	$6^1 5^1 4^6 3^8 2^3$	GAr climb	4100	1100	0.8	0.4	36	568.1s
3^{20}	GA- climb	100	600	0.2	0.2	21	3.31s	6^4	GAr climb	100	100	0.6	0.2	41	0.03s
6^{20}	GA climb	100	1100	0.8	0.2	74	22.9s	$5^1 3^8 2^2$	GAr climb	100	100	0.8	0.2	20	0.43s
4^{30}	GAr climb	100	600	0.2	0.2	40	12.4s								

For the chosen SUTs, there is no single genetic algorithm configuration that is the best

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Different values for the effectiveness of the genetic algorithm (e.g., CA size)

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Different values for the efficiency of the genetic algorithm (e.g., run time)

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The VGAs of all the improved configurations all use a climbing genetic algorithm

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GA- and GAr yield the best configuration for CA generation in 10 out of 15 SUTs

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For all SUTs, a lengthier evolutionary process improves CA generation

Experimental Results

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In 13 out of 15 SUTs, creating fewer mutated individuals leads to better CAs

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There is no common best value of P_c or m for the chosen SUTs

Experimental Results

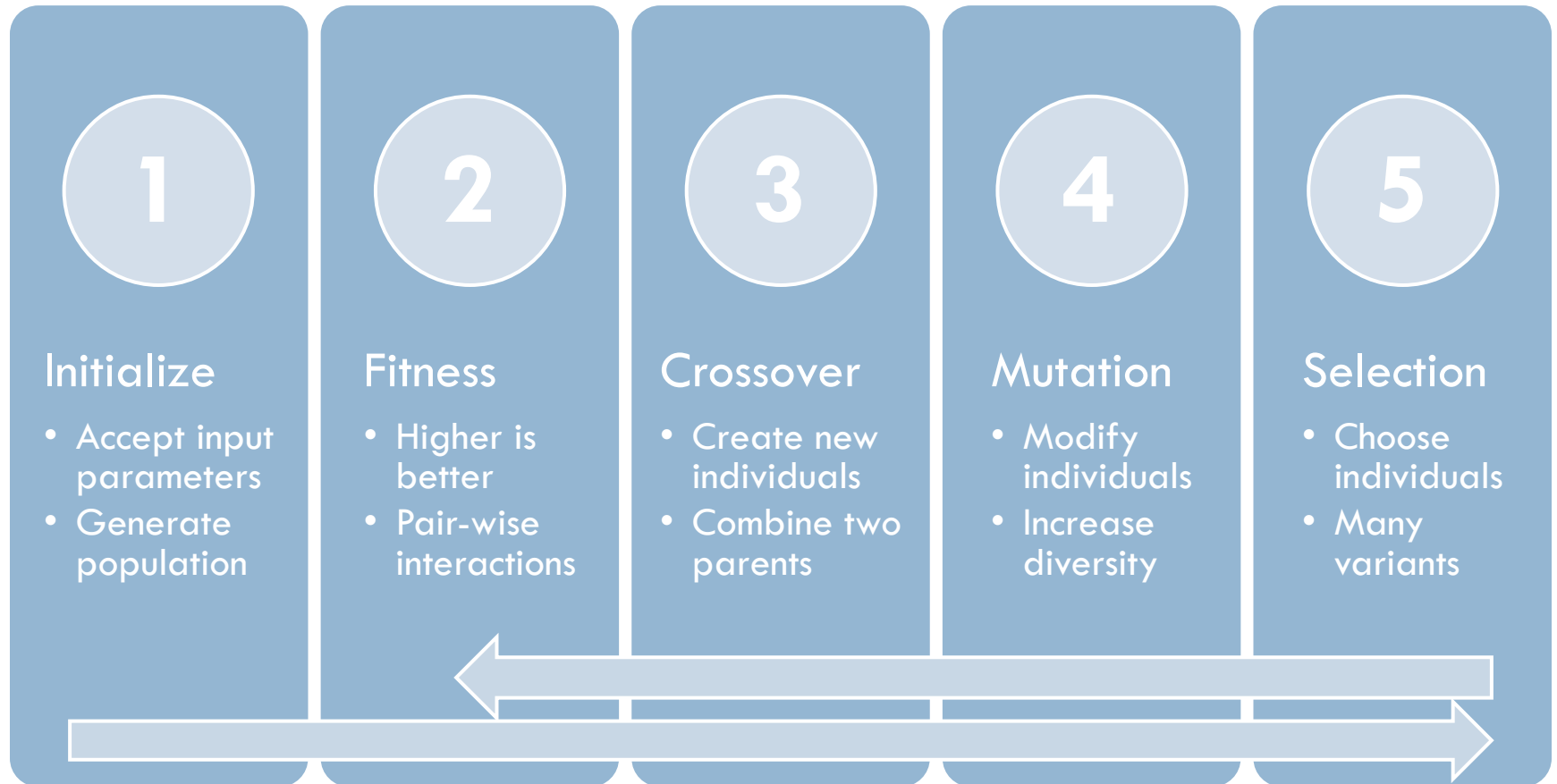
Table 3. The configurations of 15 SUTs improved by the three experiments.

SUT	VGA	m	G	P_c	P_m	CA Size	Run Time	SUT	VGA	m	G	P_c	P_m	CA Size	Run Time
4^{10}	GAr climb	100	100	0.2	0.2	28	0.234s	6^{30}	GA climb	100	1100	0.2	0.2	87	52.6s
3^{13}	GAr climb	100	1100	0.8	0.2	17	2.28s	10^{11}	GA climb	100	1100	0.8	0.2	154	19.8s
6^{10}	GA climb	6100	1100	0.2	0.2	58	402s	$7^6 6^7 5^6$	GAr climb	100	1100	0.8	0.2	82	23.5s
4^{20}	GAr climb	100	1100	0.8	0.2	35	10.1s	$8^2 7^2 6^2 5^2$	GA- climb	2100	600	0.8	0.6	70	277s
8^{10}	GA climb	2100	600	0.6	0.2	98	604s	$6^1 5^1 4^6 3^8 2^3$	GAr climb	4100	1100	0.8	0.4	36	568.1s
3^{20}	GA- climb	100	600	0.2	0.2	21	3.31s	6^4	GAr climb	100	100	0.6	0.2	41	0.03s
6^{20}	GA climb	100	1100	0.8	0.2	74	22.9s	$5^1 3^8 2^2$	GAr climb	100	100	0.8	0.2	20	0.43s
4^{30}	GAr climb	100	600	0.2	0.2	40	12.4s								

Please see the paper for additional insights concerning the experimental results

Conclusions

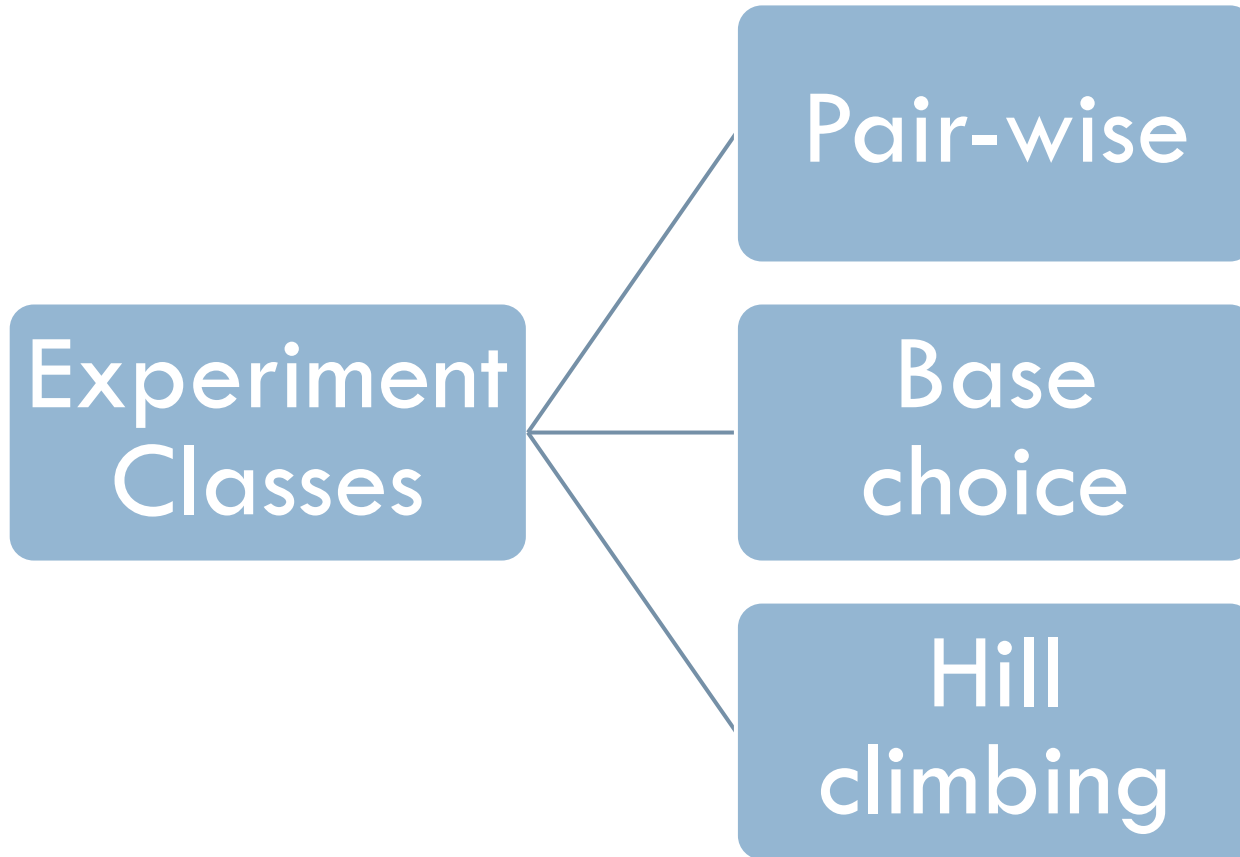
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Genetic algorithms for covering array generation

Conclusions

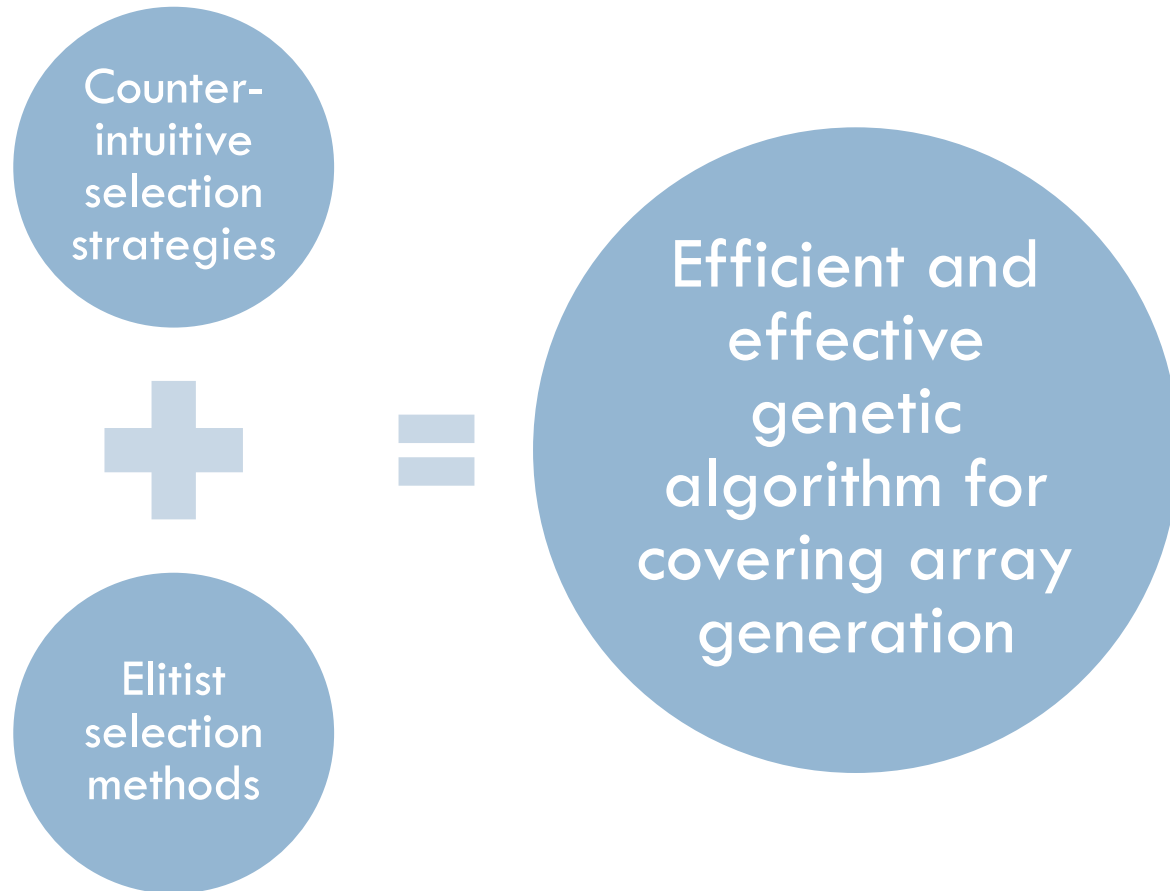
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Systematic study on the impact of GA parameters

Conclusions

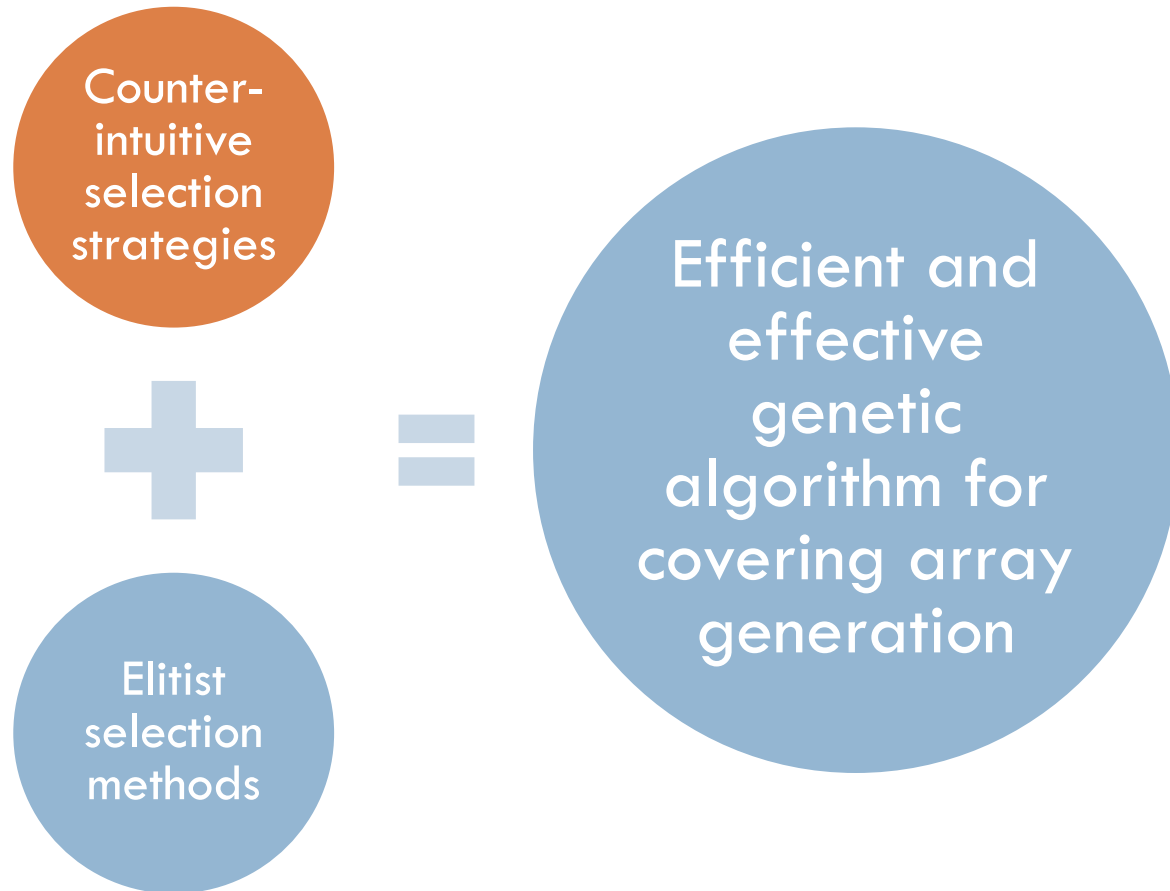
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Fundamental insights into the genetic algorithm

Conclusions

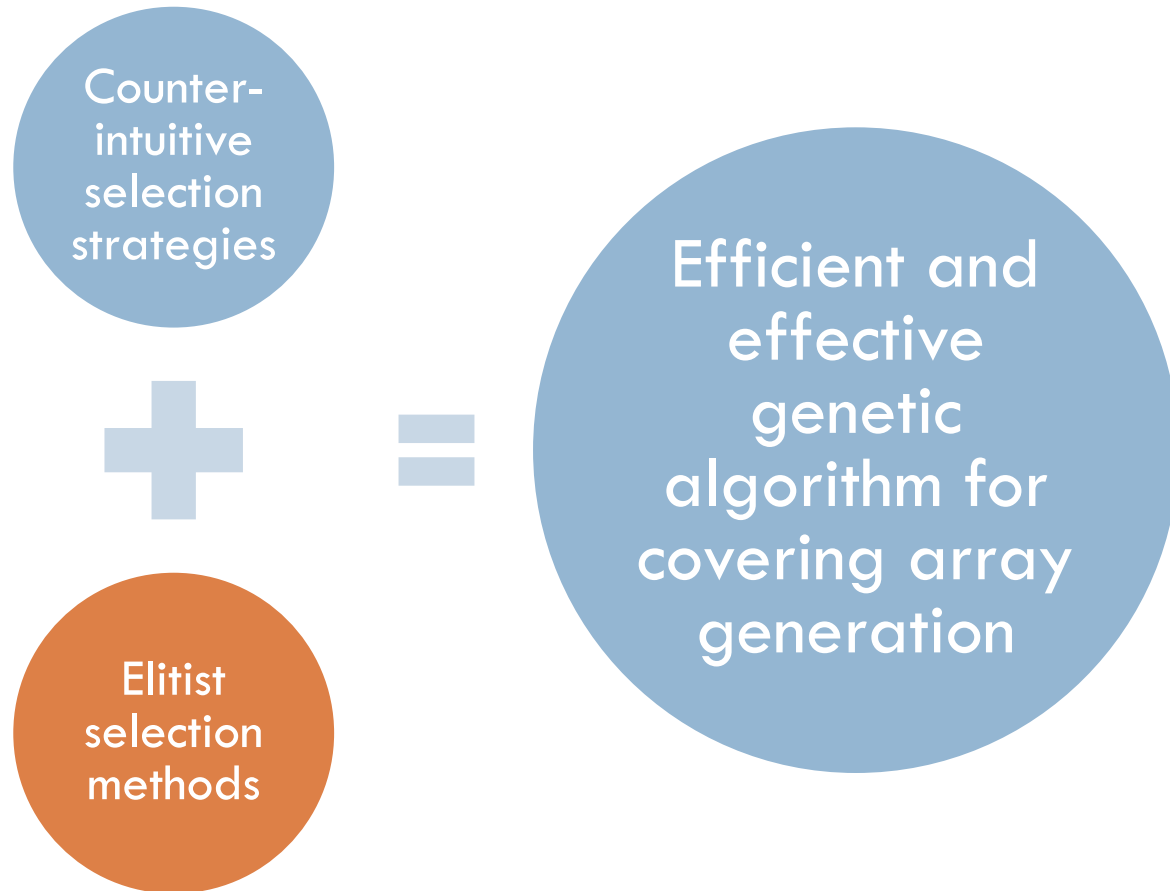
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Fundamental insights into the genetic algorithm

Conclusions

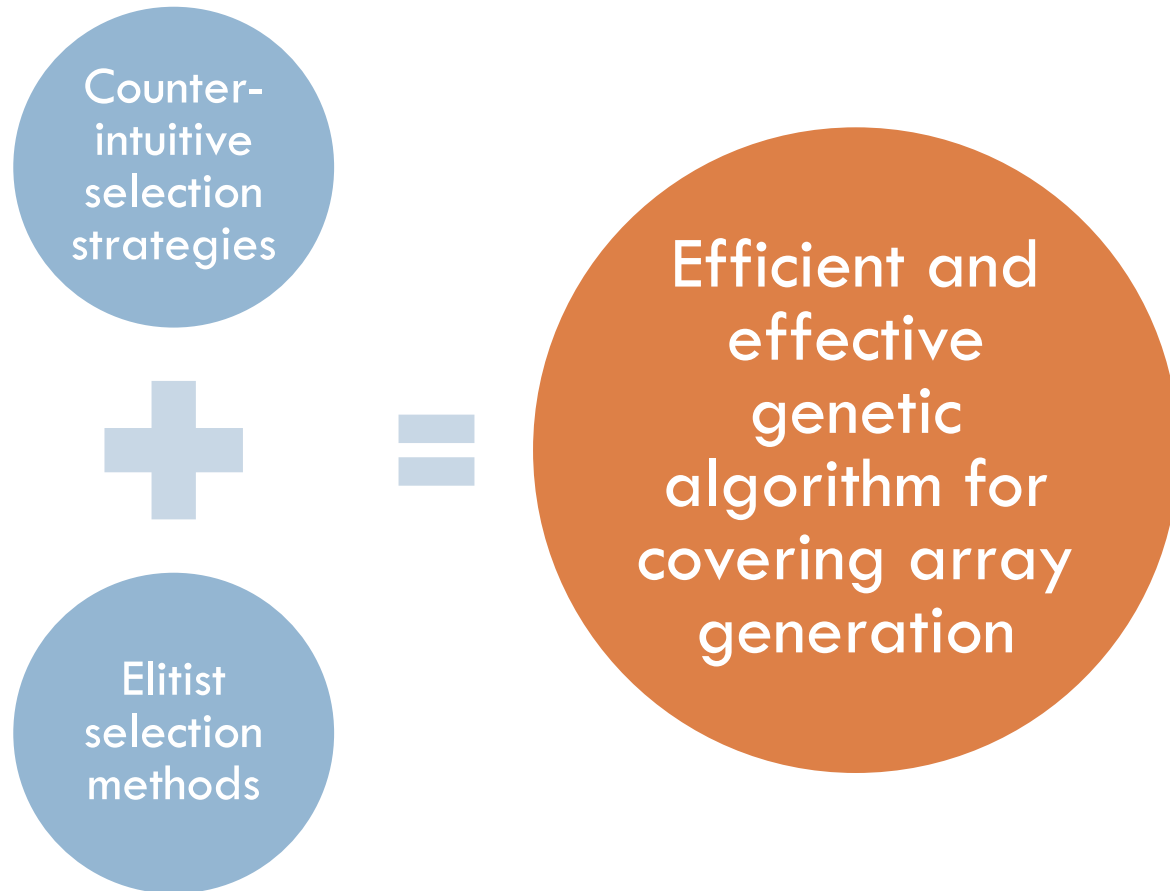
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Fundamental insights into the genetic algorithm

Conclusions

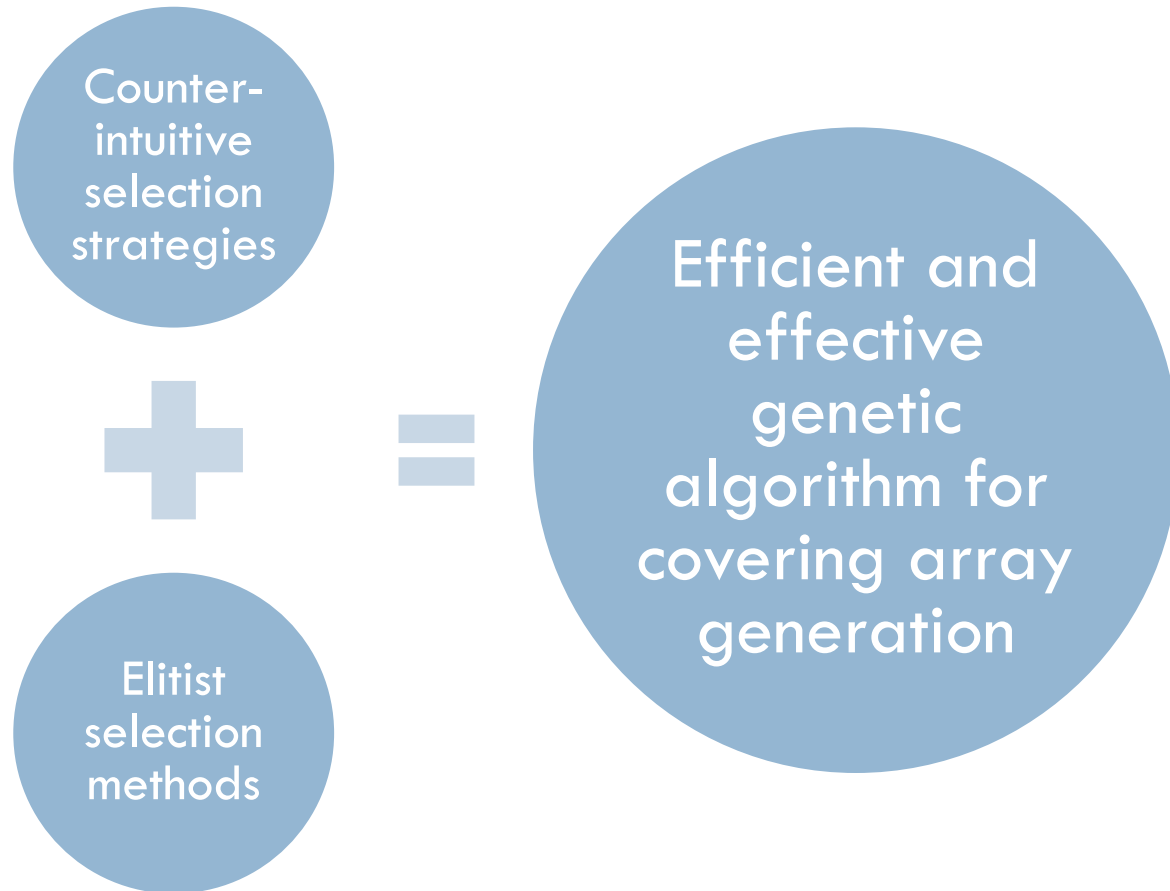
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Fundamental insights into the genetic algorithm

Conclusions

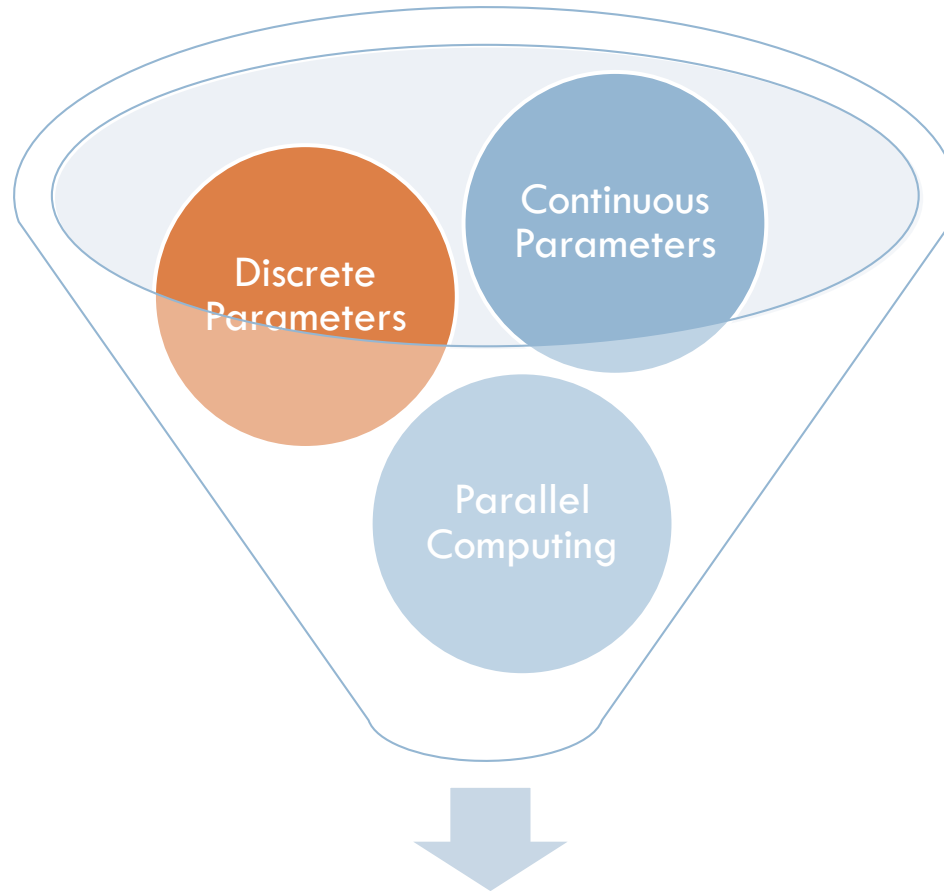
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Fundamental insights into the genetic algorithm

Future Work

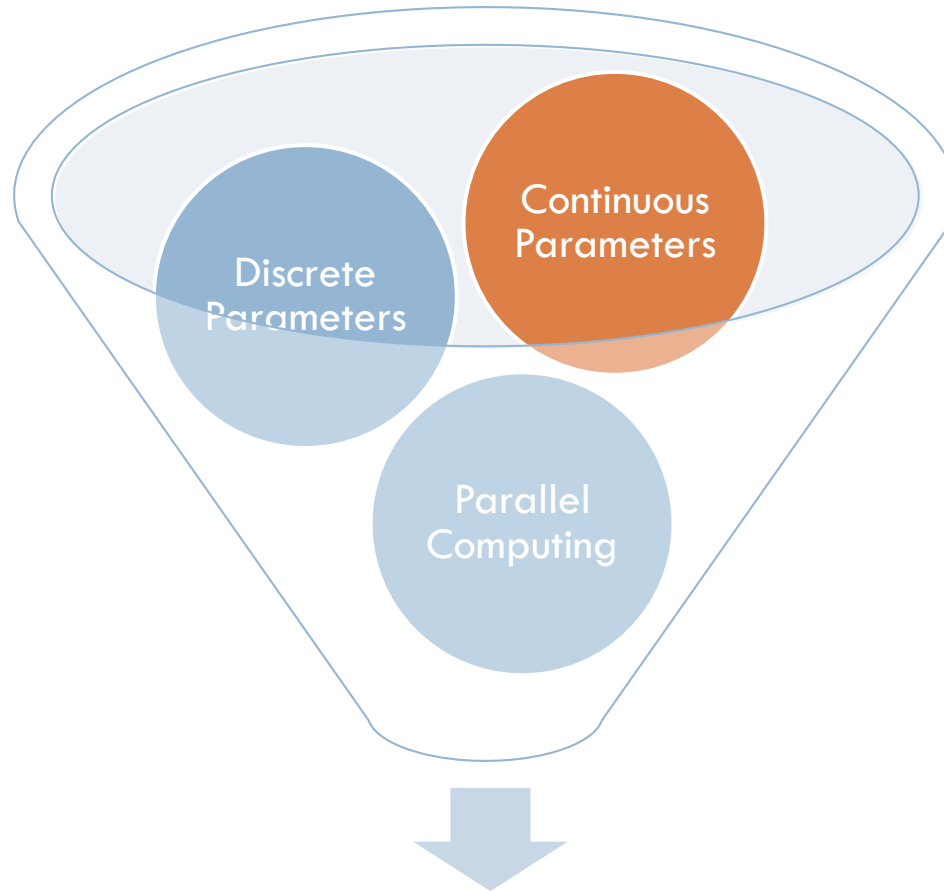
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Improved Understanding of Parameters

Future Work

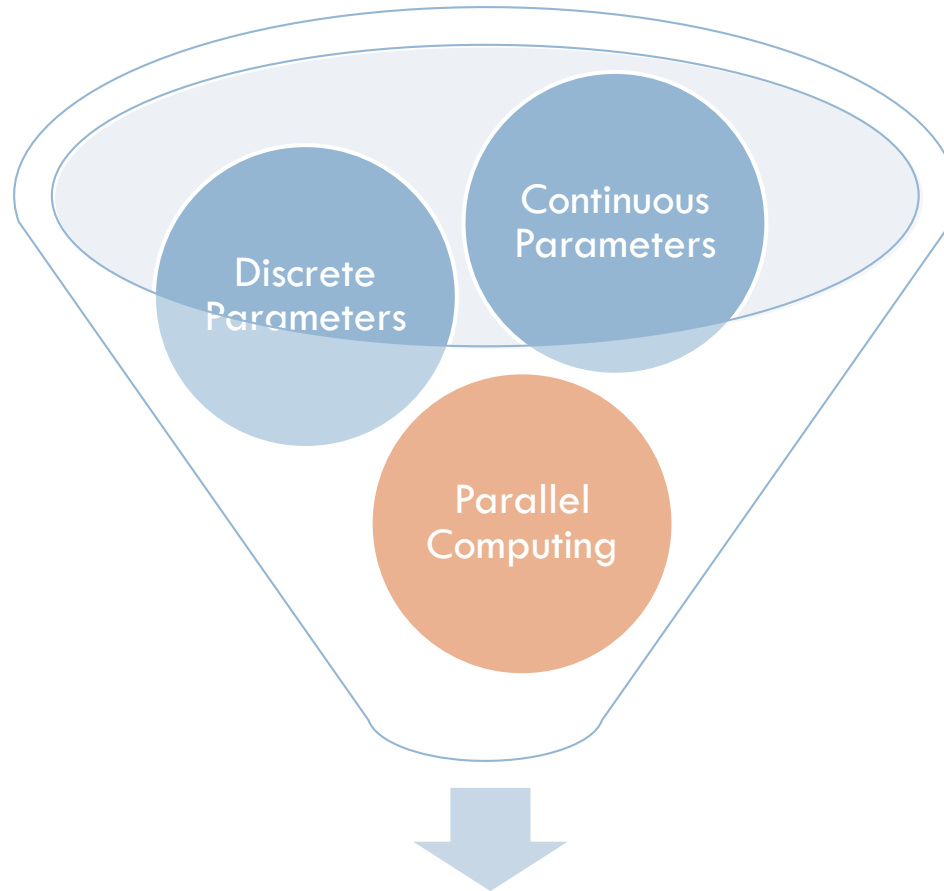
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Improved Understanding of Parameters

Future Work

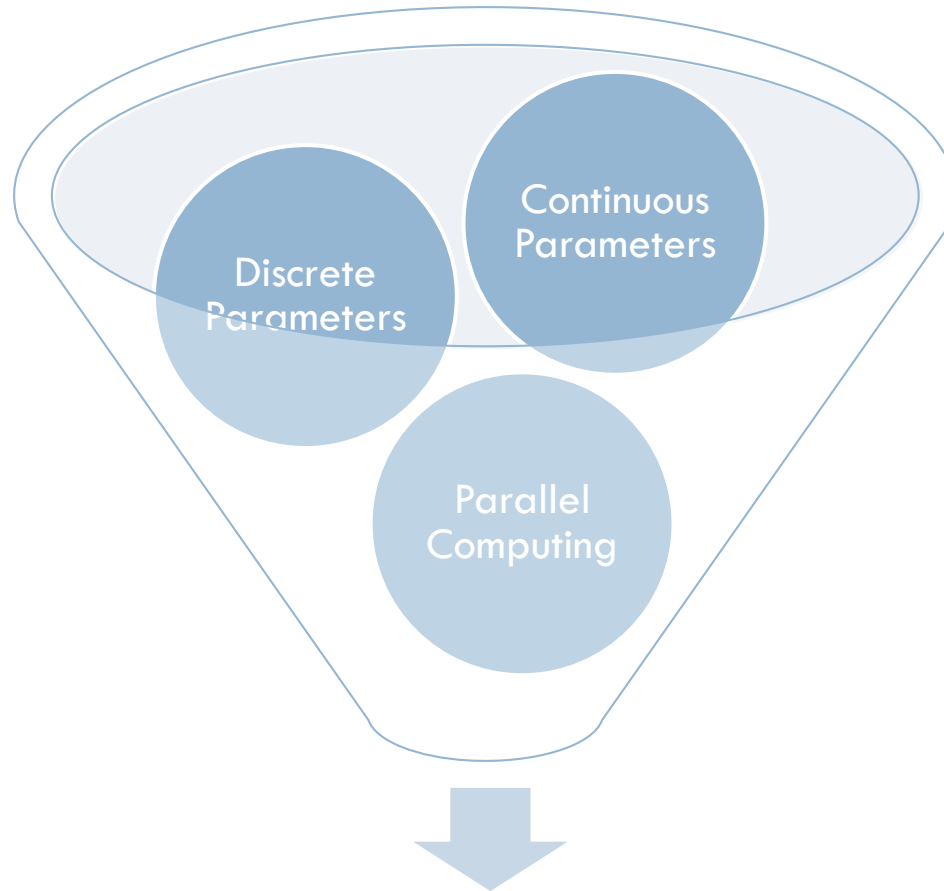
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Improved Understanding of Parameters

Future Work

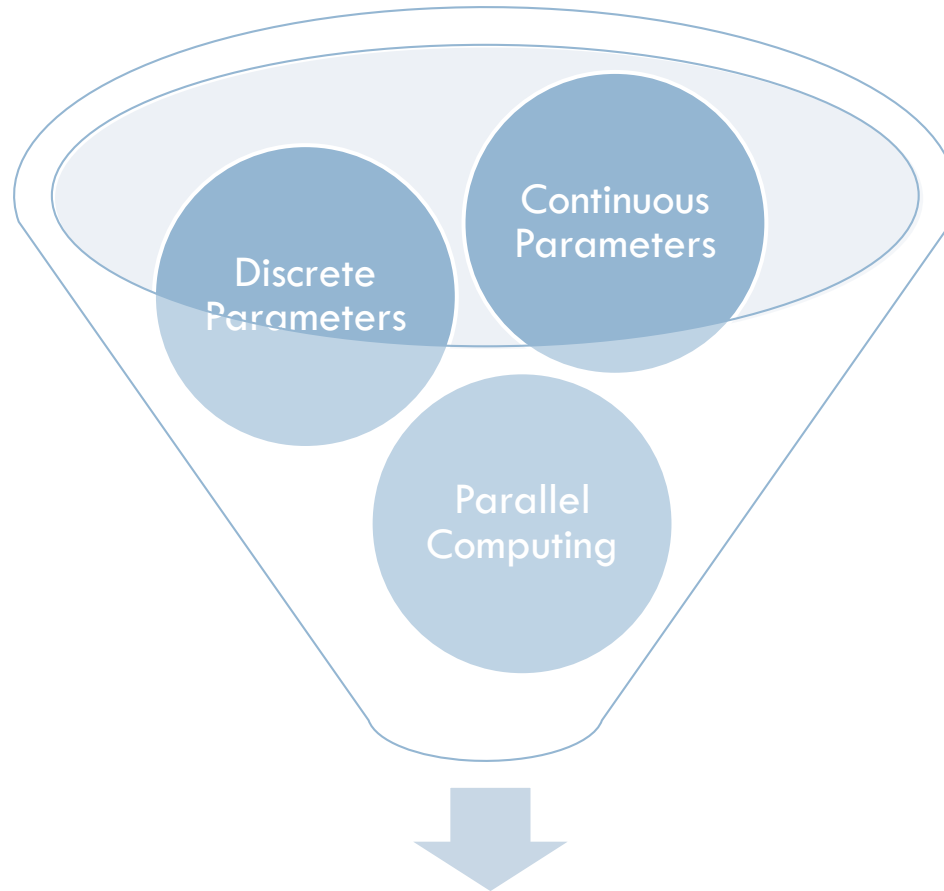
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Improved Understanding of Parameters

Future Work

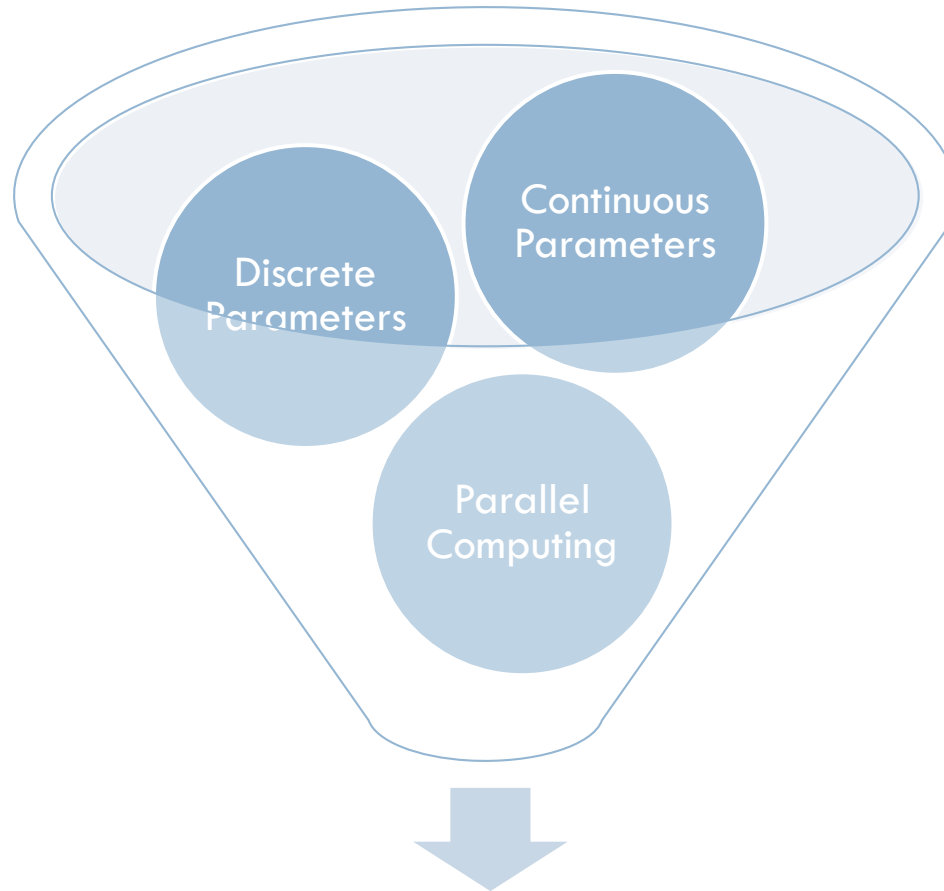
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Efficient and Effective Genetic Algorithms

Future Work

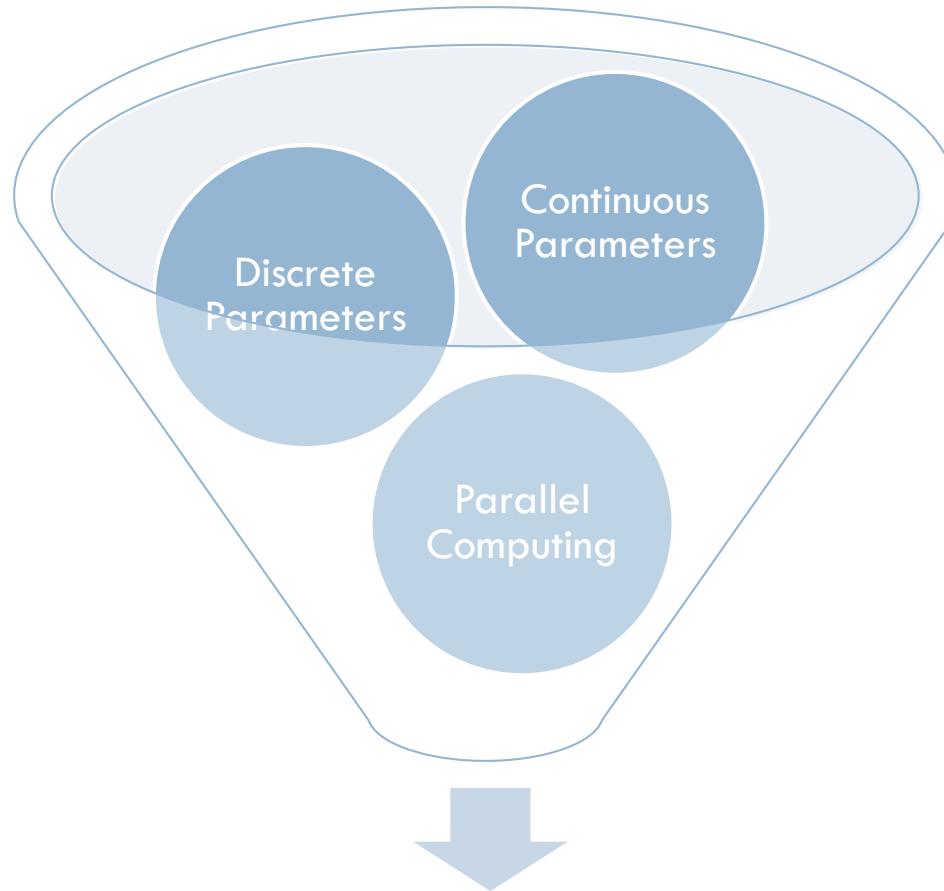
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Enhanced Covering Array Generators

Future Work

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Better Tested and Higher Quality Software

EMPIRICALLY IDENTIFYING THE BEST GENETIC ALGORITHM FOR COVERING ARRAY GENERATION

Liang Yalan, Changhai Nie, Jonathan M. Kauffman,
Gregory M. Kapfhammer, Hareton Leung

3rd International Symposium on Search Based Software Engineering
Szeged, Hungary
September 10-12, 2011

QUESTIONS OR COMMENTS?

Thank you for your attention!